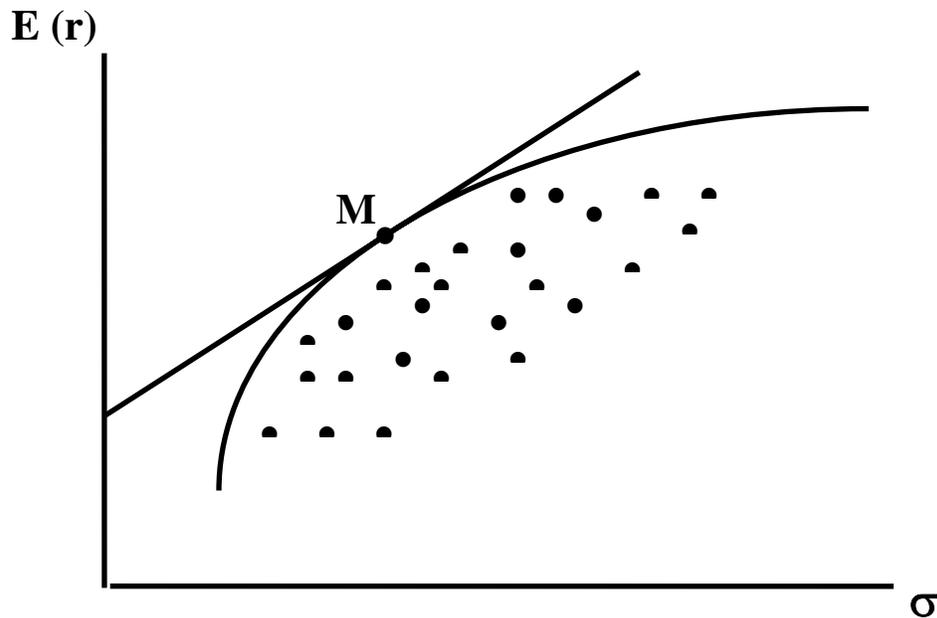


MODERN REAL ESTATE PORTFOLIO MANAGEMENT (MREPM)

REAL ESTATE IN A CAPITAL MARKET CONTEXT,
PORTFOLIO DIVERSIFICATION AND OPTIMIZATION

APPLICATIONS TO WESTERN REGIONAL
APARTMENT PORTFOLIOS



Prepared by

Lawrence A. Souza, CRE
Principal – Real Estate and Financial Economist
Johnson/Souza Group
Special Research Consultant, BRE Properties, Inc.
Doctoral Candidate, Corporate Finance, Golden Gate University
42 Jersey Street
San Francisco, CA 94114
Message: (415) 826-5661
Direct: (415) 713-0213
Lsouza@johnsonsouzagroup.com

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MODERN REAL ESTATE PORTFOLIO MANAGEMENT:

APPLICATIONS TO WESTERN REGIONAL APARTMENT PORTFOLIOS

Introduction

This report is a three part real estate portfolio research series that include: 1) Apartments in a Capital Markets Context, 2) Portfolio Diversification: Geographic and Economic Base Analysis, and 3) Modern Portfolio Theory: Arriving at Optimal Portfolio Weights. Portfolio benchmarking, exit strategies and time diversification strategies are also discussed.

This real estate capital markets research study is intended to:

- Educate real estate portfolio managers and institutional investors with capital market theory and its application to real estate portfolios.
- Identify those portfolios (individual assets and real estate markets) that have exhibited high risk-adjusted rates of return in the capital markets over time.
- Examine historical relationships between portfolio risk and return and recommend portfolios based on high historical risk-adjusted rates of return, and those portfolios that appear to have reached their cyclical bottom and are poised for value increases.

The goal of this research project is to identify the optimal portfolio weights by geographic region for an institutional (REIT) existing and future apartment portfolio. The REIT's current strategy is to acquire and develop in 14 metropolitan areas within the western region: Albuquerque, Denver, Riverside-San Bernardino, Las Vegas, Los Angeles-Ventura, Orange County, Phoenix, Portland, Sacramento, Salt Lake City, San Diego, San Francisco Bay Area, Seattle, and Tucson. The mission of this project is to identify the optimal portfolio mix based on economic, demographic, and apartment market indicators.

Real Estate in a Capital Markets Context

The first section of this report analyzes the risk-adjusted returns of competitive financial and real estate capital market assets (portfolios) and ranks them in descending order from highest to lowest. It is assumed that all capital market assets compete in the market for the finite loanable funds (savings) from surplus spending units (savers-investors) in the economy. The majority of investors is risk-averse and desires the highest return at the lowest risk.

If capital markets are assumed to be efficient, the majority of capital flows from savers and investors to those assets that have provided the highest risk-adjusted rate of return over time. Depending on the investors yield requirement, investors may also invest in assets with the highest (expected) return or invest in assets that will compensate them for taking on any additional risk. Speculators and contrarian or risk-seeking investors may invest in assets with very low returns or very high risk in anticipation of the possibility of achieving abnormal returns in the future.

This section of the study tries to prove, through objective research, that risk-averse (institutional) investors are better off investing in apartments, the West, and apartments in the West in the future. This study also looks at historical risk-adjusted returns for REITs and tries to prove that risk-averse investors are better off investing in Western apartment REITs in the future.

Portfolio Diversification and Optimization

Portfolio Diversification

The first phase of the portfolio optimization project is to measure the correlation between economic variables and apartment returns within the 14 target markets. The goal of these tests is to determine the degree to which economic or demographic variables help explain movements in apartment returns. Since apartment return data is limited, running these tests on the data that is available allows us to identify economic variables that are statistically significant in their predictability of future apartment returns.

By using economic variables produced by government agencies and collected in and on a consistent basis, we can go back as far as the late 1970s, compared to the late 1980s for apartment return data. The ability to go back to the late 1970s allows us to assemble a large sample data set. Under statistical theory, if the sample size is significantly large, it will approximate a normal (bell curve) distribution. The normality of the data is a prerequisite for using mean-variance analysis or modern (Markowitz) portfolio optimization techniques.

Portfolio Optimization

The second phase of the portfolio diversification study is to identify optimal portfolio allocations that achieve the highest expected rate of return at the lowest level of risk for the portfolio. This phase determines the optimal portfolio weighting by geographic area. The goal of this phase is to compare the REIT's portfolio diversification to a risk-return weighted ("target") portfolio, then, from the variances, optimal v.s. actual allocations, a recommended acquisition strategy is structured to eliminate, to the extent possible, the risk of excess geographic concentration in the portfolio.

Time Diversification

The third phase of the portfolio diversification study is to identify stable real estate cycles across metro areas. Investment in metro areas with long expansion cycles and short contraction periods reduces total portfolio return volatility (risk) and increases risk-adjusted returns (expected return). The determining factor in low long-term risk-adjusted returns is infinite land availability; resulting in inventory supply shocks, and higher probabilities that the metro area will enter hyper-supply (new construction) phases more often. Unconstrained real estate markets are more volatile, resulting in lower long-term total returns, occupancy rates, and effective rent growth. Supply constrained markets have limited land availability, reducing supply shocks, and allowing the market to recover sooner. Weighting the portfolio with a bias toward supply-constrained markets reduces portfolio volatility and maximizes risk-adjusted return.

RISK MANAGEMENT AND INSTITUTIONAL REAL ESTATE SECURITIES

Institutional Real Estate Capital Markets

Current trends impacting institutional real estate capital markets are the accumulation of large saving pools, continued securitization of real estate assets and decreasing capital flows into direct real estate investments.

This shift away from direct real estate ownership, managed and operated by real estate pension advisors, to indirect real estate ownership, managed and operated through real estate investment trusts (REITs) and real estate operating companies (REOCs), has caused many of these firms to reorganize and develop sophisticated risk management systems.

The goal of these systems is to manage growth and mitigate dividend yield and stock price volatility. Lower volatility and correlations between stocks and bonds provides institutional investors with opportunities to reduce overall portfolio risk, warranting additional allocations into REIT/REOC securities.

Additional allocations are projected to accelerate the development of the institutional real estate securities market. Real estate investment markets are notorious for their inefficiency, failures and asymmetric information; as a result, the institutional real estate securities market should provide benefits to the economy by allocating real estate capital flows more efficiently.

The efficient allocation and intermediation of real estate investment capital through REITs/REOCs provides deficit spending units with low cost capital and surplus spending units with higher investment returns. Lower social costs and higher public welfare are achieved through the elimination of high transaction and information costs associated with direct real estate investment.

Trends in Institutional Real Estate Capital Markets

Institutional Real Estate Holdings

The importance of real estate as a legitimate asset class for investment and diversification purposes is exemplified by its contribution to total world wealth. According to Ibbotson Associates, in 1991, of the over \$43.8 trillion in total world wealth, 48% is held in real estate, compared to 27% in bonds and 19% in equities; and of the over \$15.4 trillion in total U.S. wealth, 39% is held in real estate, compared to 23% in bonds and 28% in equities. According to these percentages most individual investors are over weighted and most institutional investors are under weighted in real estate from a global portfolio perspective.

Although institutions are under weighted in real estate, they do hold a significant portion of the total U.S. real estate market. According to Equitable Real Estate, May 1996, institutional investors owned \$1.28 trillion of the \$3.2 trillion total U.S. real estate market. Pension funds account for \$114.4 billion (43%) and REITs account for \$56.1 billion (22%) of the \$254.4 billion

in total equity holdings. Pension funds currently own 10.7% and REITs own 8.0% of the \$1.2 trillion institutionally owned commercial real estate market.

As of June 1996, institutional holdings of direct real estate measured by the NCREIF Property Index totaled \$53.7 billion, over 35% in retail, 32% in office, 15% in apartments and 12% in warehouse properties. Institutional investors--pension funds, life companies and mutual funds--now control well over 50% of the outstanding shares of publicly traded real estate investment trusts.

Capital Flows into Real Estate

Capital flows into real estate is determined through the diversification benefits received by including it in a multi-asset portfolio, but is mainly due to investor expectations for future financial performance. Many investors are becoming weary of the stock market's ability to continue to rise and are feeling that the market might be over bought. If equities are over priced, providing historically low dividend yields compared to other asset classes, then real estate assets are under priced in comparison.

This disequilibrium in (arbitrage) pricing between the two capital markets will cause an increasing flow of investment capital into the real estate market, driving down current yields for real estate and drive up dividend yields for stocks. Capital flows into the real estate market will continue until risk-adjusted returns and arbitrage pricing spreads between the two asset classes are equalized and traded away.

Potential capital flows into real estate are enormous. The accumulation of new capital for real estate investments comes mostly from private savings of corporations and individuals. According to a recent ULI article, from 1990 to 1995, corporate net income rose 6.5% per year from \$581 billion to \$798 billion, personal saving rose 7.3% per year from \$170 billion to \$241 billion, and gross savings (public and private) rose 8.0% from \$722 billion to \$1.06 trillion. As of the first quarter of 1996 savings equaled investment, real private fixed investment totaled \$1.06 trillion.

A significant portion of this savings and investment went into direct real estate investments and real estate related financial instruments. As of the second quarter of 1996, the NCREIF Property Index totaled over \$53.68 billion, up 6.4% per year from \$39.36 billion in the second quarter of 1991; and from 1990 to 1995, the NAREIT index rose 46.0% per year from \$8.7 billion to \$57.5 billion. As of October 1996, REITs raised a record \$8.36 billion in 1996 through 100 secondary offerings. This compares with \$7.32 billion in 93 offerings in 1995 and just \$3.94 billion in 52 secondary offering in 1994.

Supply and demand for real estate assets has become more balanced over the past five years and rents in most metro areas support new construction. Although the capital markets are currently aligned with supply and demand fundamentals, industry observers are concerned that public market and institutional investors will over react to improved market conditions, increasing the supply of investment capital, and creating capital flow pressures the market can not absorb.

The affect of these capital flows could drive down current capitalized yields on real estate assets to the point where new construction is justified to obtain higher yields. As the magnitude of capital flowing into the market increases, the probability of over building runs high. The risk of over building could parallel that seen in the mid-to-late 1980s.

Emerging Institutional Real Estate Securities Capital Markets

Institutional investors are drawn to the REIT/REOC markets to create core portfolios, to balance the diversification of a private market portfolio, to co-invest, to arbitrage between public and private markets and to access larger property types and niches unavailable in the private markets.

According to AEW Research, the average pension fund allocation targets 50% equities 45% in fixed income and 5% in other investments. Most pension funds admit their target real estate allocations are not fully funded and individuals are under-allocated evidenced by the only \$2.5 billion in REIT -dedicated mutual funds, compared to a total of \$1.3 trillion in all stock mutual funds.

An adjustment by institutions and individuals to a 6% allocation of their total investment portfolio would cause institutional investors to increase their investment flows into real estate by \$100 billion and individuals by \$65 billion, a total of \$165 billion; this, along with the ability to take advantage of the up-and -down REIT structures, could push REIT market capitalization well above \$200 billion. With financial institutions and infrastructure already in place, the REIT market could quadruple in size over the next five years.

The ability of REITs/REOCs to raise capital in four dimensions (private equity and debt and public equity and debt) gives them a significant competitive advantage over other market participants.

As an emerging capital market, the REIT/REOC market has advantages over other markets that have developed in the past: the Southeast Asian equity markets of the early-1990s and the junk bond markets of the early-1980s.

The advantages REITs/REOCs have are capitalizing in a financial system with well established monetary policies and controls, financial reporting and disclosure rules, financial intermediaries and institutions and a developed financial market infrastructure with the latest information processing and telecommunications technologies. This system allows REITs/REOCs to raise capital in the public markets at relatively low costs and allows their issues to trade in liquid and established stock markets at relatively low transaction and trading costs.

In comparison, the emerging Southeast Asian markets of the early-1990s saw significant flows of capital but were unable to handle these flows due to lack of monetary controls and central bank independence and inefficient, illiquid and thinly traded capital markets. These characteristics were reflected in the volatility of stock prices and the inability of investors to exit the markets due to currency controls and lack of market participants.

In the early-1980s the U.S. saw the emergence of the junk bond market. This market, like the Asian equity market, was established due to relatively low yields being offered on comparative financial instruments at the time. These low yields were a result of the recessions of 1980 and 1982. Low current yields caused investors to look toward more riskier markets for returns. The establishment of the junk bond market provided investors with the yields they wanted and corporate raiders with finance capital needed for hostile takeovers. Eventually, the lack of market capitalization and liquidity collapsed the junk bond market through successive Wall Street scandals and the S&L crisis.

Optimal Size for Market Efficiency

It is assumed that over the next five years the size of the REIT market will capitalize to the point where up to \$1.0 billion dollars in shares can be traded within a reasonable time period. This will allow investors to convert their investments to cash without significant loss of value. Increased liquidity of the REIT/REOC market has been accompanied by an increase in share price, but increased liquidity will make these shares more sensitive to changes in the expectations of market liquidity.

Growth in market capitalization has been driven by high expected returns in the stock market, low volatility in U.S. stock markets, continuation of rising capital flows from defined contribution plans into stock mutual funds, better alignment of interests between management and investors and public market information and valuation.

REITs are being accepted more and more by institutional and individual investors as the investment vehicle of choice due to low capital requirements for constructing a well-diversified multi-asset real estate portfolio.

The growth of publicly traded real estate securities has improved the dissemination of data available to public and private market investors, information previously deemed proprietary and closely guarded. REITs/REOCs are continuing to make improvements in reporting, full disclosure standards and timeliness of new releases.

Liquidity of the public institutional real estate securities market will be dependent on improved information flows from an increasing number of securities analysts, traders and rating agencies. Increased liquidity that comes from a larger capitalized market will cause real estate security prices to become more sensitive to expected capital market in-flows. This sensitivity will cause higher volatility in REIT/REOC share prices. Volatility in share prices, as in interest rates, will spur the development of a real estate backed derivative securities market.

This market will improve market efficiency by allowing investment managers to hedge portfolio risk, investment bankers to hedge price movements prior to new issues and arbitrageurs to speculate between the options and stock markets. Increased speculator activity provides more liquidity to the market by improved pricing through the reduction of arbitrage spreads between the two markets.

Institutional Trading of Real Estate Securities

Increased capitalization, information flows and liquidity has sparked institutional interest in real estate securities. REIT/REOC shares have been perceived to have lower liquidity than large-cap issues. Lower liquidity requires higher yields, the current S&P index dividend yield is roughly 2.0% compared to 7.0% for REIT stocks. Large institutional shareholders have been averse to smaller-cap REIT/REOC stocks due to problems associated with trades moving the price, but in 1996 there were 97 REITs with capitalizations over \$200 million, the size of most mid-size cap stocks. REITs are fairly heavily traded relative to their market size, but are less liquid by dollar size compared to large-cap stocks.

Over the next five years market liquidity is projected to increase as market capitalization grows. The REIT market is forecast to grow at a rate of 15% per year, based on historical averages. By the year 2007, REIT market capitalization could reach \$300 billion and by 2017 over \$1.4 trillion. Efficient market conditions in the REIT market are just now being achieved, this is evidenced by rising volume, institutional block trades and off-market transactions.

Friction Less Portfolio Construction and Diversification

U.S. stock markets are the most liquid markets in the world due to standards of information disclosure and number of transactions and participation, leading to low cost trading. Liquid capital markets provide for friction less portfolio construction and diversification. Increased disclosure and dissemination of financial information allows REIT/REOC shares to be bought or sold quickly at prices close to or at their current market value. With lower transaction and search costs associated with stocks, large institutional investors can implement tactical asset allocation programs to increase or decrease exposures to various sectors of the real estate market, while maintaining a core portfolio.

The ability of the investor to construct a securities portfolio of assets with varying unsystematic risks allows for risk reduction through portfolio diversification. The movement from a direct real estate investment portfolio to a REIT/REOC portfolio does expose institutional portfolios to greater systematic real estate risk., because of the location specific characteristics of the real estate asset in a direct investment portfolio, but lowers the systematic risk of the overall mixed-asset portfolio due to real estates positive correlation with inflation and negative correlation with stocks and bonds.

Risk Management and Institutional Real Estate Securities

With the potential for enormous flows of capital into the real estate capital market REITs/REOCs must be able to manage these capital infusions and rapid growth associated it. REITs/REOCs need to rethink their organizational structure and implement well thought out risk management strategies. As capital flows increase there will be mounting pressure by institutional shareholders for these firms to accumulate properties and develop a well diversified portfolio. The value of REIT/REOC shares will come mainly from the perceived strength of their management teams and quality of their real estate portfolio.

Risk Management Strategies: An Integrated Top Down/Bottom Up Approach

As participation and involvement of institutional investors grow, REIT/REOC management teams will be required to develop and implement well designed risk management strategies. The core of these strategies will be an integrated top down and bottom up approach to portfolio construction and management.

The top down approach will be research driven. This approach draws heavily on the resources and skill sets of its research department, and emphasizes the utilization of real estate market and economic forecast models to select product types and geographic regions for potential acquisitions.

Institutional investors, along with their advisors and consultants, screen and select REITs/REOCs based on their strategic plans and alliances, management teams, historical performance and market capitalization; and their ability to maximize cash flow, manage the balance sheet and access capital markets. Premiums are being paid and additional funds are flowing to those firms having the organizational structures in place to handle large flows of investment capital and have risk management policies and a well defined portfolio strategy in place to mitigate portfolio risk from geographic and economic over concentrations.

The ability to diversify and manage the core real estate portfolio is reflected in the firms funds from operations (FFO) and stock price volatility. Firms that meet or exceed FFO projections and have lower stock price volatility compared to their peers receive larger allocations from risk-averse institutional investors.

To mitigate FFO and stock price volatility, REITs/REOCs must vertically integrated and have successfully diversified their portfolio by geographic region and economic concentration, taking advantage of low to negative correlations between markets and employment over time.

Vertical Integration

First, the firm must be vertically integrated. The firm must be vertically integrated with a high-quality seamless portfolio-property management and reporting system. The goal of this system is to facilitate information flows up from the property level and down from senior management. This type of organizational structure eliminates problems associated with decision making based on incomplete (asymmetric) information, and makes for a more complete model of information disclosure and dissemination.

With property management functions in-house the firm can take advantage of administrative and management economies of scale, achieving administrative cost savings through efficient payroll, property and portfolio level accounting and reporting systems. Firms with large and diversified portfolios obtain local market efficiencies and synergies obtained through a regional focus and use of regional managers. Regional managers in association with property managers allow the firm to have better property level focus and management over the life of the property.

Geographic Diversification Strategy

Second, firms must diversify their portfolio geographically. Geographic diversification reduces the risk of revenue loss caused by regional economic shocks. The goal is to have a large enough portfolio concentrated geographically to obtain economies of scale, but not overly concentrated to the point where economic shocks significantly disrupt portfolio revenue streams. Geographic diversification is only one method of immunizing the real estate portfolio from over concentrations in economic risk.

Economic Base Diversification Strategy

The second method of immunizing the portfolio is to diversify across industries or employment concentration. By measuring the correlation between employment trends within each target market, and testing for correlations across time and economic groupings, portfolio management can determine the degree to which shared employment concentrations and shared employment movements between markets impact the portfolio. Using Economic Base Diversification (EBD) analysis a diversification strategy with existing properties and potential acquisitions can be developed.

Using geographic diversification strategies in conjunction with economic base analysis, an optimal portfolio structure can be identified and allocations achieving the highest expected return at the lowest possible risk can be calculated. The goal of this strategy is to compare the company's portfolio diversification to an evenly weighted ("proxy") portfolio. From the calculated variances optimal portfolio allocations can be derived. These variances help guide future portfolio acquisitions and dispositions, eliminating the risk of excessive geographic or economic concentration.

Catastrophic Risk Underwriting

The third method of immunizing the portfolio is to diversify by product quality and geographic region with respect to the probability of catastrophic loss. An enterprise at risk is characterized by the fact that the fundamental nature of the operation is such that expenditures may exceed receipts during some accounting periods in the normal course of operation.

For example, over \$35 billion in damage was wreaked in the 20 largest disasters in recorded Bay Area history, with the largest component coming from earthquakes, \$15.4 billion or about 45% of the total damage. Areas of major concern are areas along the Hayward and San Andreas faults. It is estimated that if there were a major earthquake along the Hayward Fault, it would force more than 300,000 Bay Area residents from their homes.

The goal of assessing and systematically managing catastrophic risk is to determine what degree the real estate portfolio income stream is at risk of losses. This is done by conducting deterministic and probabilistic loss analysis by property, geographic area and type of construction. Estimated costs of damage based on these probabilities determines optimal insurance (premium) coverage that protects the properties without over insuring.

By assessing the economic impact of catastrophic events on portfolio income, the REIT/REOC can devise a risk mitigation program consisting of either self-insurance (sinking fund), single insurer coverage, multiply insurer coverage or a multiple property and/or insurer strategies that minimize insurance premiums while maximizing coverage.

Property Level Diversification Strategy

The bottom up approach to portfolio construction and management is submarket and product specific. This strategy is implemented by the acquisitions department and overseen by senior officers. This strategy relies heavily on the acquisition team's experience in any given market and type of real estate being acquired. The value of this approach is reflected in the quality of local market contacts and relationships and the ability to move viable deals through the pipeline.

The goal of this approach is to assess risks inherent in property-specific investment decisions, and understand the potential risks and returns of those decisions. This approach focuses on risk factors inherent by property type and class; factors such as vacancy loss, property life cycle and the potential use of leverage.

A bottom up approach evaluates property performance based on market risks: inventory size, new construction, supply constraints, economic and demographic changes affecting tenant demand and investor sentiment. The end product is an evaluation system that prices assets and market risk premiums accurately within a portfolio context.

Economic Efficiencies and Wealth Maximization

Over the next ten years, the REIT/REOC market will free up a significant amount of capital trapped in a relatively illiquid real estate market. Freeing up and dissemination of investment capital through securitization creates an efficient system of allocating scarce resources and provides a stimulus for long term sustainable economic growth. Efficiencies through securitization come from lower transaction and financing costs and providing capital to a capital-starved sector of the economy.

Through the use of real estate backed securities benefits accrue to providers and users of capital. Investors will benefit by having access to markets once priced out of and the ability to move in and out of the markets quickly and cheaply. Overall, the more intensive use of real estate capital provides higher returns for investors and a lower cost of capital for users in the long run.

LITERATURE REVIEW

MODERN REAL ESTATE PORTFOLIO THEORY (MREPT)

Introduction

Over the past twenty years, modern capital market theories have been applied to real estate portfolio development and management with mixed results. The difficulty in applying this theory is that underlying capital market assumptions do not hold-up well in real estate markets. This is due to information asymmetries, high transaction costs, illiquidity, uniqueness of asset characteristics, private property rights, and tax and land-use legislation. The market is efficient, but it takes longer for it to arrive at market clearing prices.

Theoretical constructs of modern capital market theory are extremely important when analyzing real estate as an asset class, and diversifier in a mixed asset portfolio:

- Expected Returns (Competitive)
- Variance of Returns (Lower)
- Covariance of Returns (Lower)
- Random Walk (Weak-Form)
- Efficient Market Hypothesis
- Systematic and Unsystematic Risks

Modern Portfolio Theory (MPT)

Harry Markowitz, Modern Portfolio Theory

Modern Portfolio Theory (MPT) was introduced by Harry Markowitz with his paper "Portfolio Selection" which appeared in the 1952 Journal of Finance. Thirty-eight years later, he shared a Nobel Prize with Merton Miller and William Sharpe for what has become a broad theory for portfolio selection and corporate finance.

Modern Portfolio Theory explores how risk averse investors construct portfolios in order to optimize market risk against expected returns. The theory quantifies the benefits of diversification. Out of a universe of risky assets, an efficient or optimal portfolio can be constructed.

Each portfolio on the efficient frontier offers the maximum possible expected return for a given level of risk. Investors should hold one of the optimal portfolios on the efficient frontier and adjust their total market risk by leveraging or deleveraging that portfolio with positions in the risk-free asset. In a highly simplified world, the market portfolio sits on the efficient frontier, and all investors hold that portfolio, leveraged or deleveraged with positions in the risk-free asset.

Modern Portfolio Theory provides a broad context for understanding the interactions of systematic risk and reward. It has profoundly shaped how institutional portfolios are managed, and motivated the use of passive investment management techniques. The mathematics of MPT is used extensively in financial risk management.

The Markowitz approach requires a large sample size of returns to approximate a normal distribution. Once enough data is collected, and is normal in nature, mean-variance analysis can be used to approximate the optimal allocation depending on the pre-determined weight constraints.

Modern Real Estate Portfolio Theory (MREPT)

Mueller, Pauley, and Morrill explain why institutional investors today must continue to consider both private direct real estate investments, as well as public or securitized forms of ownership, in order to develop an optimal portfolio that includes appropriate subcategories of real estate assets. Market depth, liquidity, asset quality, diversification, and price volatility are all considered strategically used portfolio management criteria in this must primer for the diversified portfolio investor (Mueller, 1995).

Institutional real estate investment - primarily pension reserve assets - grew rapidly in the 1980s. The fiduciary demands of a growing asset pool coupled with disappointing results in the latter half of the decade led to an increasing interest in the application of Modern Portfolio Theory (MPT) to the management of large-scale real estate portfolios. This paper reports the results of a study conducted in mid-1990 that surveyed the 426 largest institutional portfolios on portfolio management practices relating to diversification strategies, risk measurement, and evaluation of investment returns (Louargand, 1992).

The survey replicated several measures gathered by Webb in a 1983 survey to assess the rate of acceptance or utilization of ideas and techniques in the portfolio management community. Results indicate that change is perhaps slower than might be expected. Real estate performance measures have become more sophisticated in the past seven years with a shift away from accounting type measures toward fully discounted measures, including several variations on the Internal Rate of Return (IRR).

Risk-adjustment techniques have changed to the extent that portfolio managers have a greater likelihood of using sensitivity analysis, but few other innovations are widespread. Only a small percentage of respondents use traditional tools of MPT-based analysis, but the majority are cognizant of recent developments in the literature that attempt to show alternative methodologies for achieving true diversification within real estate portfolios (Louargand, 1992).

The results indicate that change is gradual and that some practices that have been discredited in the academic literature for many years may still be evident in the institutional community.

Styles of REIT Portfolio Management

Investment styles and return objectives in real estate portfolio management have focused on higher return strategies: wealth creation, value added, income enhancement, and incremental risk. The ability of the REIT to achieve these goals through direct real estate (active) portfolio management is determined by management skills and experience. Due to real estates illiquidity and asymmetric information flows, portfolio diversification and optimization strategies are followed over multiple periods. Where it may take a stock managers weeks to adjust the portfolio to new optimal weights based on new return and risk information, it may take the real estate portfolio managers up to three years to adjust the portfolio, depending on size, market conditions, etc. (Stoesser, 2000).

When developing large institutional real estate portfolios, one of the main objectives is to identify and target outperforming markets based on high risk-adjusted rates of return. Factors used in determining target markets are: real estate market opportunities, demographic attributes, and market size. Due to the capital intensity, high transaction and information costs, most direct real estate portfolio managers underwrite properties on a buy and hold basis, extending the investment horizon. This allows the manger to focus on long-term cyclical labor market and demographic trends. For example, the emergence of the echo-boomer and retirement of the baby boomers are expected to support apartment markets in the future (**Han, 1996**).

There are many factors contribution to the supply of apartments: tax policy, capital availability, estimated demand by developers, etc. Statistically significant variables determining new apartment supply are: mortgage interest rates, housing affordability index, employment change, vacancy rates, and taxes (Giliberto, 1995).

Real Estate Portfolio Development

Institutional real estate portfolio development is conducted in an integrated top-down/bottom-up fashion. Top-down analysis starts with national market and economic analysis, regional market and economic analysis, local market and economic analysis, and property level analysis; and then the process starts back up again.

At the national level risks analyzed are: inflation, industrial production, risk premiums, term structures, business cycles, taxes, etc.; at the regional level risks analyzed are: unsystematic risks, employment based and growth, demographic trends, income levels and growth, and vacancy rates; at the local level risks analyzed are: employment base and growth, demographic trends, income levels, vacancy rates, construction levels and costs, space utilization rates, and taxes; and at the property level risks analyzed are: physical characteristics, location and site characteristics, lease characteristics, property management expertise, and financing (Lieblich, Pagliari, 1996).

Opportunities for Diversification

Historically, real estate has shown negative correlations with financial assets due to lease inflation indexation, and correlations between real estate markets have been low due to industrial concentration by geographic area. The ability to add real estate to a stock or bond portfolio, or diversify across geographic-industrial class, provides diversification benefits to portfolio managers. Volatility in institutional real estate portfolios emanates from two sources: 1) high risk/ return ratios, and 2) capitalization rate pressure due to oversupply conditions or declining effective demand. Allocations to real estate asset portfolios are dependent on contributing returns and perceived risks associated with acquisitions (Bruce, 1991).

Portfolio Exit strategies

There are many reasons why institutional real estate portfolio managers dispose of properties. The new institutional imperative for disposition strategies of real estate portfolios is generated by pressures on management in the following areas: re-emphasis on core business, product and geography; reaction to poor performance of real estate portfolios; new risk-based capital standards imposed by banks and institutional equity investors; and rapidly declining property income and asset values. Disposition strategies include: single asset management sales, portfolio auctions, pooled asset portfolio sales, bulk portfolio sales, securitized asset pooled asset sales, or UPREITing the portfolio into the public market (Buckley, 1994).

RESEARCH DESIGN I

REAL ESTATE IN A CAPITAL MARKETS CONTEXT

Introduction

Apartment portfolio construction has been out of favor for some time due to concerns of overbuilding in some markets. We believe that long-term apartment fundamentals are solid and investors have overreacted to short-term market conditions. Over the long run, apartments have provided investors with the highest risk-adjusted rates of return of any real estate asset class.

Some apartment markets whose long-term returns have been heavily discounted due to excessive volatility may have been oversold by investors, providing opportunities for contrarian or risk-seeking investors. Those apartment markets whose returns have been negative or flat for quite some time, reaching their cyclical bottom, could be poised for rapid income and capital appreciation as they move into the recovery phase of their cycle. It is expected that these portfolios will see rapid income appreciation induced by a healthy national economy and capital appreciation spurred by large institutional (REIT and pension fund) capital inflows.

These capital flows are attracted to apartment portfolios because of their high income returns and undervalued status in the capital markets compared to other competitive financial market assets (stocks and bonds). Through the use of capital market analysis, we can identify which portfolios will continue to attract risk-averse, risk-neutral, and speculative capital over time.

This section of the study identifies those portfolios (assets, real estate markets and real estate investment trusts) that have exhibited high risk-adjusted returns in the capital markets over time, and assumes that these portfolios will continue to attract capital flows from risk-averse investors.

These portfolios are plotted within an efficient frontier context by expected return and risk (standard deviation). This analysis examines historical relationships between risk and return and recommends portfolios based on high risk-adjusted returns, and those portfolios that appear to have reached their cyclical bottom and are poised for value increases.

Investment portfolios analyzed in this study are:

- Competitive Capital Market Assets
- Competitive Real Estate Portfolios by Asset Class
- Competitive Real Estate Portfolios by Region
- Competitive Apartment Portfolios by Region
- Competitive Real Estate Portfolios in the Western Region
- Competitive Real Estate Portfolios by Western Regions
- Competitive Metropolitan Apartment Portfolios in Western Region
- Competitive Apartment Real Estate Investment Trust Portfolios

This section of the report is divided into five sections: methodology, discussion of results, conclusions and recommendations, assumptions and appendices.

- The **Assumptions** section defines the theoretical constraints for the capital market and efficient frontier models.
- The "**Methodology**" section introduces the procedures taken to arrive at the order of portfolios ranked by risk-adjusted return.
- The "**Discussion of Results**" section elaborates on why these portfolios rank the way they do, and why they are positioned the way they are within an efficient frontier context. This section also identifies which portfolios are attractive to risk averse, risk neutral and risk seeking investors.
- The "**Conclusions and Recommendations**" section summarizes the findings and makes recommendations for future portfolio investment based on the results of the analysis and strategy of the investor. Lastly, this section briefly discusses future portfolio research.
- The **Appendix** gives the efficient frontier graphs; statistical rules of thumb, diversification analysis and variance analysis, back-testing graphs and tables, qualitative factors, optimization and regression results, risk-adjusted return tables; total return tables; standard deviation tables; total return graphs; and return deviation graphs, by competitive portfolio (market); and definitions and data sources.

Before discussing the results of the study we must make some assumptions. First, capital markets are efficient and capital flows move freely at no or low transaction costs. Second, the majority of investors are risk-averse. Generally, most institutional investors are risk-averse, but they can also be considered risk neutral, risk seeking, speculative or contrarian depending on their yield requirements, investment horizon and risk tolerance. Third, total returns are normally distributed over time.

Assumptions

Efficient Capital Markets

The capital markets are assumed to be efficient in modern portfolio theory because it consists of a large number of rational, profit-seeking and risk-averting investors. They compete freely with each other in estimating the future value of individual assets and markets.

Since any change affecting a given asset or market is quickly known it is therefore rapidly reflected in the price of the asset to which it relates. The capital market is said to be efficient because it quickly incorporates any new change or event affecting the value of the asset.

It is assumed that capital markets are efficient in that prices adjust rapidly to the infusion of information and capital flows, and prices fully reflect all information regarding the asset. Markets are efficient in that:

- A large number of profit-maximizing participants are concerned with the analysis and valuation of the asset, and that these participants operate independently of each other.
- New information regarding assets comes to the market in a random fashion, announcements are generally independent of one another.
- Asset prices (intrinsic value) that prevail in the market at any time should be an unbiased reflection of all currently available information, including risk. Therefore, returns implicit in the price reflect the risk involved, so the expected return is consistent with risk.
- Investors adjust asset prices rapidly to reflect the effect of new information. Although price adjustments are not always perfect, it is unbiased, and over and under adjustments average out over time.

Under these assumptions, a single asset or portfolio of assets is considered to be “efficient” if no other asset or portfolio of assets offers higher expected return with the same (or lower) risk, or lower risk with the same (or higher) expected return.

Efficient Frontier

The first step in the portfolio (market) selection process is to determine the risk-return opportunities available to the investor. The efficient (minimum-variance) frontier is a graph of the lowest possible portfolio (asset or market) variance that can be attained for a given portfolio expected return. The efficient frontier is a graphic presentation of the pairing between expected returns and minimum-risk portfolios (assets or markets).

The second step in the portfolio (market) selection process is to search for portfolios with the highest reward-to-variability ratio.

The efficient frontier is that set of portfolios that has the maximum return for every given level of risk, or the minimum risk for every level of return. The shape of the efficient frontier assumes for risky assets is generally such that one has to tolerate more and more risk to achieve higher returns.

The slope of the efficient frontier decreases steadily as you move up the curve. This tendency implies that equal increments of added risk, as you move up the efficient frontier, will add progressively less of an increment in expected return (declining returns to scale).

Capital Flows

Capital allocators make investment decisions under uncertainty, therefore seek to achieve the best possible trade-off between risk and return. The capital allocation decision is the choice between putting investment funds in safe but low return assets versus risky but higher-return assets.

Risk-free assets, such as T-Bills, are short-term in nature making them insensitive to interest rate fluctuations. An investor can lock in a short-term nominal return by buying a bill and holding it to maturity. The inflation uncertainty over the course of a few weeks, or even months, is negligible compared with the uncertainty of other risky investments.

Institutional investors follow a top-down approach to capital allocation. Since capital flows freely across markets, historical and new information is incorporated into asset prices instantaneously and there are no or low transaction costs, institutional investors can adjust their real estate portfolio positions relatively rapidly, therefore they are constantly adjusting their portfolios to minimize risk or maximize risk-adjusted returns.

Under these assumptions capital flows are disciplined and will continue to flow to those assets or portfolios offering the highest long-term risk adjusted returns.

Investing in a REIT that is diversified within a region can be considered a passive investment strategy. Forces of supply and demand in large capital markets may make such a strategy a reasonable choice for many institutional investors; therefore, by developing a clear, well defined and communicated portfolio and risk management policy, and institutional real estate manager (REIT) can continue to attract institutional capital flows.

Investor Preferences

Most investors try to determine the best risk-return opportunities available in the market, try to avoid risk and demand a reward for engaging in risky investments. The reward is taken as a risk premium, an expected rate of return higher than that available on alternative risk-free investments. Investors make personal trade-offs between risk and expected return, and is dependent on their welfare or utility function. The proper way to measure the risk of a portfolio is to assess the volatility of total returns over time.

Investors determine where they want to be within the efficient frontier in terms of their utility function and attitude toward risk. They would then select a portfolio based on their risk preferences. No portfolio is dominated by any other portfolio, they all have different return and risk measures, and returns increase with risk.

Risk-averse investors penalize expected return on risky portfolios to account for risk, the greater the risk the larger the penalization. Depending on the investors' utility function, higher welfare is achieved from higher expected returns and lower welfare is achieved from higher return volatility. The extent to which the variance of returns lowers investor welfare depends on the degree of risk aversion, the more risk-averse an investor is the larger the risky investment is penalized.

- **Speculators** invest in assets with considerable business risk and expect a commensurate gain beyond the risk-free alternative. Speculators invest in spite of the risk involved because they perceive a favorable risk-return trade-off.

- **Risk-neutral** investors judge risky prospects solely by their expected rates of return. The level of risk is irrelevant to the risk-neutral investor, meaning there is no penalization for risk, the risk-adjusted rate of return is simply its expected rate of return.
- The **risk lover** is an investor who is willing to gamble on an investment, adjusting the expected return upward to take into account the “fun” of confronting the prospect’s risk.

Normality of Returns

Modern portfolio theory, for the most part, assumes that asset returns are normally distributed, therefore, total returns on portfolio investments are assumed to be normally distributed over time. This is a convenient assumption because the normal distribution can be described completely by its mean and standard deviation, justifying mean-variance analysis. The argument has been that, even if individual asset returns are not exactly normal, the distribution of returns of a large portfolio will resemble a normal distribution quite closely.

This is how one can best describe the uncertainty of portfolio rates of return. The expected rate of return in this study is an equally (time) weighted average of returns, the weights being the probabilities.

The characterization of risk is implied by the nature of the probability distribution of returns. The idea is to describe the likelihood and magnitudes of “surprises” (deviations from the mean) with as small a set of statistics as is needed for accuracy.

Methodology

The Capital Market or Efficient Frontier Analysis (EFA) consists of four separate but related phases.

Phase I: Portfolio Selection

Phase II: Calculate Expected Return and Standard Deviations

Phase III: Plot Portfolios by Expected Return and Standard Deviation

Phase IV: Rank Portfolios by Risk-Adjusted Returns

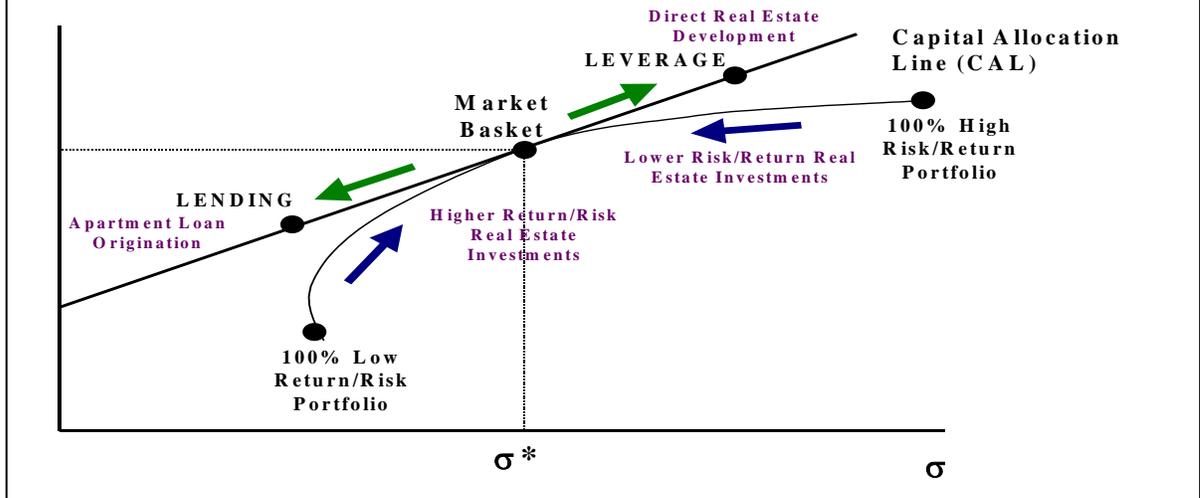
Note: For this study a portfolio is an asset class, an asset class by region or a real estate investment trust.

- Rankings by relative performance is simply a sort in descending order of portfolios by risk-adjusted returns. Risk-adjusted returns are portfolio expected or average returns over the sample time period divided by the standard deviation of total returns for this same time period. Please refer to the Appendix and the notes in the risk-adjusted return tables for sample time periods. **Caution: Short sample time periods may produce higher sampling errors.**

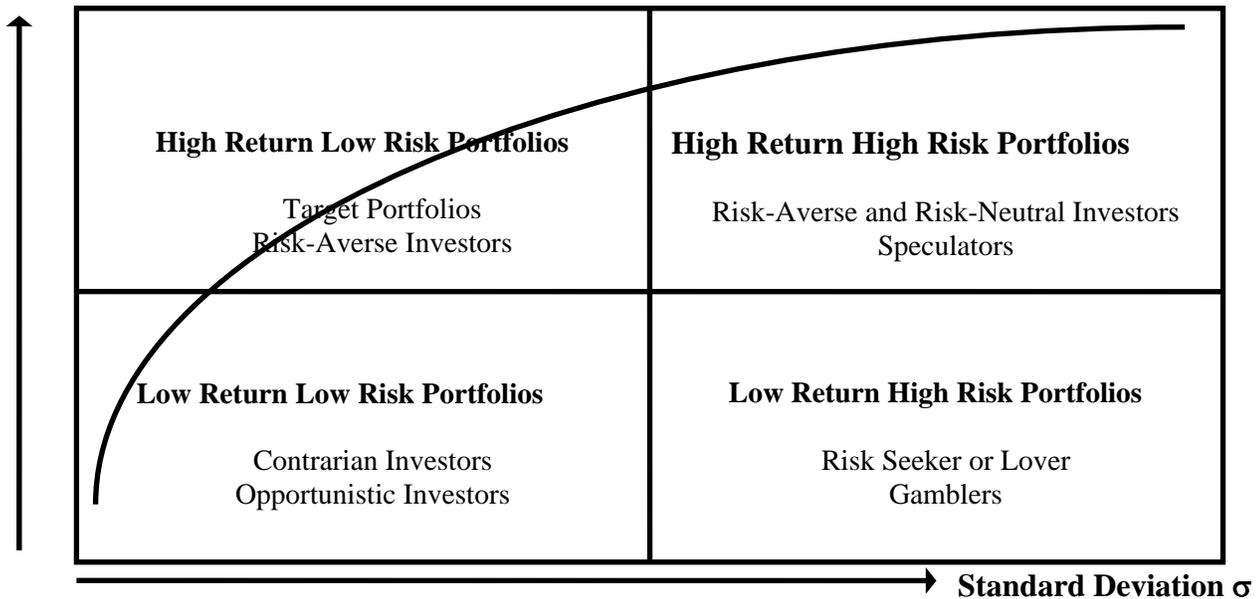
- Risk-adjusted returns give the number of units of return for each given unit of risk for each portfolio. Risk-adjusted returns measure portfolios that have the maximum return for every unit of risk, or the minimum risk for every unit of return. This allows for comparison across portfolios after controlling for risk. Please refer to the risk-adjusted return tables and total return graphs, in the Appendix for more details.
- Risk is the variance or standard deviation of expected returns. It is a statistical measure of the dispersion of returns around the (mean) expected value; that is, a larger value for the variance or standard deviation indicates greater dispersion, all other factors being equal. The ideal is that the more dispersed the returns, the greater the uncertainty (risk) of those returns in any future period. Please refer to the risk-adjusted return tables, sorted by standard deviation, and total return deviation graphs in the Appendix for more details.
 - The total return deviation graphs illustrate the degree of volatility in the portfolio's total return, the degree of the portfolio's real estate cycle trough or peak, and allows for identification of where the portfolio is within its current real estate cycle.
- The Efficient Frontier plots are graphical illustrations of where each market is located within a competitive capital market context.

Institutional Real Estate Capital Allocation Line

Movements Along the Efficient Frontier



Mean Expected Return $E(r)$



- According to capital market theory, portfolios exhibiting high long-term relationships between risk and return are located in the upper right-hand corner of the graph, and portfolios exhibiting low long-term relationships between risk and return are located in the lower left-hand corner of the graph.
- Target portfolios for risk-averse investors are those portfolios that exhibit high stable long-term returns with low standard deviations. These portfolios are located in the upper left-hand corner of the graph.
 - Some risk-averse (institutional) investors would be willing to accept lower returns for lower risk. These portfolios are located in the lower left-hand corner of the graph.
- Target portfolios for contrarian or opportunistic investors are those that have exhibited low total returns and low risks. These investors are anticipating higher future returns at lower risk levels.
 - Risk seeking investors, or gamblers, are willing to invest in portfolios with high risk and low returns in anticipation of the possibility of achieving high returns in the future to compensate for high risk levels. These portfolios are located in the lower right-hand corner of the graph.
 - Some opportunistic investors would be willing to accept lower returns for higher risk if they felt the portfolio was under valued in the capital markets, leading to arbitrage opportunities.

Please refer to the efficient frontier graphs in the Appendix for more details.

Data sources for portfolio total returns and standard deviations came from the National Council of Real Estate Investment Fiduciaries (NCREIF), Koll/National Real Estate Index and Dean Witter Reynolds Investment Banking Unit.

- The NCREIF real estate indexes are appraisal based and are a representative sample of institutional real estate holdings by asset class and region. Total return and standard deviation information was compiled from quarterly return statistics. Total returns include income return and capital appreciation.
- The Koll/National Real Estate Index is a biannual/quarterly survey based on a sample of properties by asset class and metro area. Total returns and standard deviations were derived by adding together the biannual/quarterly percentage change in sales price per square foot with the biannual/quarterly capitalization rate to arrive at a total return figure.

- Dean Witter Reynolds Investment Banking Unit provided total dividend yields and percent change in stock prices for the competitive REITs to arrive at a total return figure on a quarterly basis.

**NATIONAL COUNCIL OF REAL ESTATE INVESTMENT FIDUCIARIES (NCREIF)
GEOGRAPHIC REGIONS**

East	<u>Northeast</u>	<u>Mideast</u>
	Maine	Delaware
	New Hampshire	Maryland
	Vermont	Washington D.C.
	Massachusetts	West Virginia
	Rhode Island	Virginia
	Connecticut	North Carolina
	New York	South Carolina
	New Jersey	Kentucky
	Pennsylvania	
Midwest	<u>East North Central</u>	<u>West North Central</u>
	Wisconsin	Minnesota
	Michigan	Iowa
	Ohio	Missouri
	Indiana	Kansas
	Illinois	Nebraska
		North Dakota
		South Dakota
South	<u>Southeast</u>	<u>Southwest</u>
	Tennessee	Oklahoma
	Mississippi	Arkansas
	Alabama	Louisiana
	Georgia	Texas
	Florida	
West	<u>Mountain</u>	<u>Pacific</u>
	Montana	Washington
	Idaho	Oregon
	Wyoming	California
	Colorado	Alaska
	New Mexico	Hawaii
	Arizona	
	Nevada	

Discussion of Results

By using the Capital Market or Efficient Frontier Model (EFM):

- Portfolios that appear most attractive to (institutional) investors over the long run based on high risk-adjusted returns are those shown in the Risk Averse section of the tables below.
- Portfolios most attractive to risk neutral investors appear in the Risk Neutral section of the tables. These portfolios are those exhibiting the highest long-term expected return.
- Portfolios attractive to the opportunistic, contrarian or risk seeking investors appear in the Risky section of the tables.
 - These portfolios are those whose long-term returns have been heavily discounted due to excessive volatility over time and may be poised for significant capital inflows to compensate for excessive risk levels.

Risky real estate portfolios could also be seen as those whose returns have been negative or flat for quite some time, reaching their cyclical bottom, and are poised for rapid income and capital appreciation as they move into the recovery phase of their cycle. It is expected that these portfolios will see rapid income appreciation driven largely by a healthy national economy and capital appreciation driven largely by institutional (REIT and pension fund) capital inflows.

These capital flows are attracted to real estate portfolios due to their high income returns and undervalued status in the capital markets compared to other competitive financial market assets (stocks and bonds).

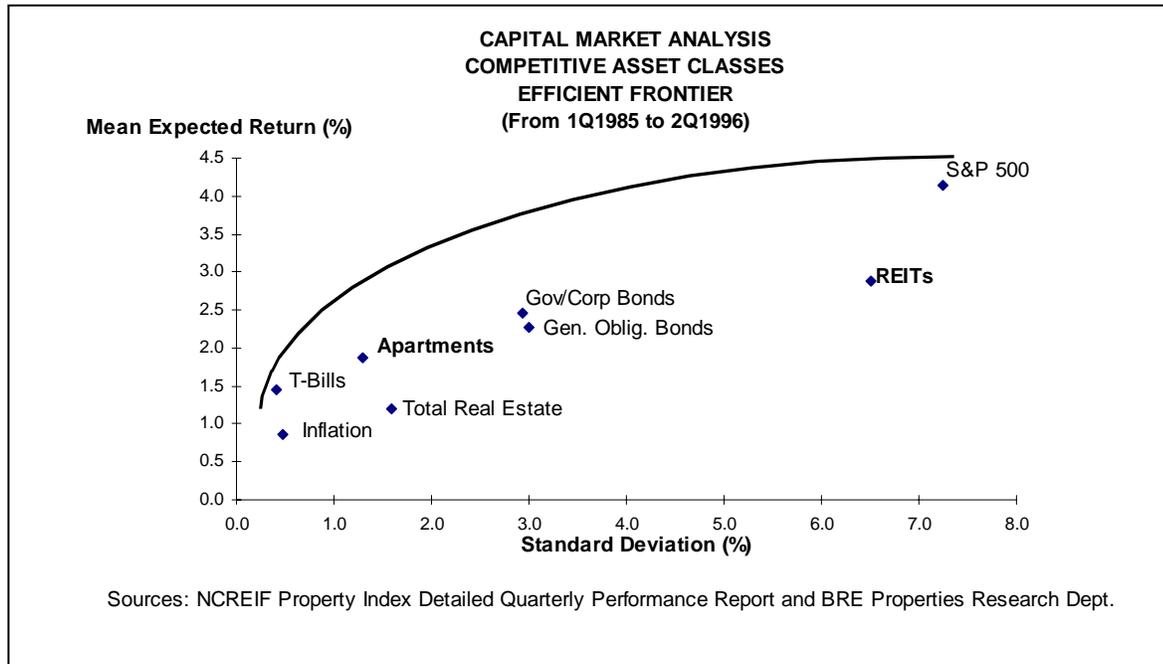
Through the use of capital market analysis we can identify which portfolios will continue to attract risk-averse institutional capital over time and which portfolios will attract speculative capital over time.

Apartments in a Competitive Capital Markets Context

As illustrated in the table below, capital market portfolios exhibiting the highest risk-adjusted returns are T-Bills, Inflation and Apartments. These portfolios have exhibited low levels of risk in comparison to their rates of return over time.

Inflation could be considered as an investment in commodities or real assets such as gold/silver, antique furniture, art, etc. Since apartments have been a highly desirable investment over the years, along with stable income returns, they also rank high in risk-adjusted returns. Due to their low volatility, or sensitivity to rising or falling inflationary expectations, these asset classes should continue to be viewed as inflationary hedges and attract large flows of institutional capital.

Over time risk neutral investors have benefited from the bull market in stocks (S&P500), capitalization of the REIT market and appreciating bond prices due to low and declining interest rates. Although these portfolios have provided the highest rates of return over time they have also been the most risky. These portfolios will continue to attract large flows of speculative capital.



COMPETITIVE FINANCIAL ASSET CLASSES			
ASSET CLASS	STANDARD DEVIATION	MEAN EXPECTED RETURN	RETURN/RISK RATIO
<u>Risk Averse</u>			
91 Day T-Bills	0.4	1.4	3.5
Inflation (CPI)	0.5	0.9	1.8
Apartments	1.3	1.9	1.5
<u>Risk Neutral</u>			
S&P 500	7.2	4.1	0.6
REITs	6.5	2.9	0.4
Gov./Corp.Bonds	2.9	2.5	0.8
<u>Risky</u>			
REITs	6.5	2.9	0.4
S&P500	7.2	4.1	0.6
Gov.Oblig. Bonds	3.0	2.3	0.8

Note: Please refer to the Appendix for the efficient frontier, risk-adjusted return table, total return graphs, and total return deviation graphs for more details.

Apartments in a Competitive Real Estate Capital Markets Context

As illustrated in the table below, real estate portfolios exhibiting the highest risk-adjusted returns are apartments, retail and warehouse.

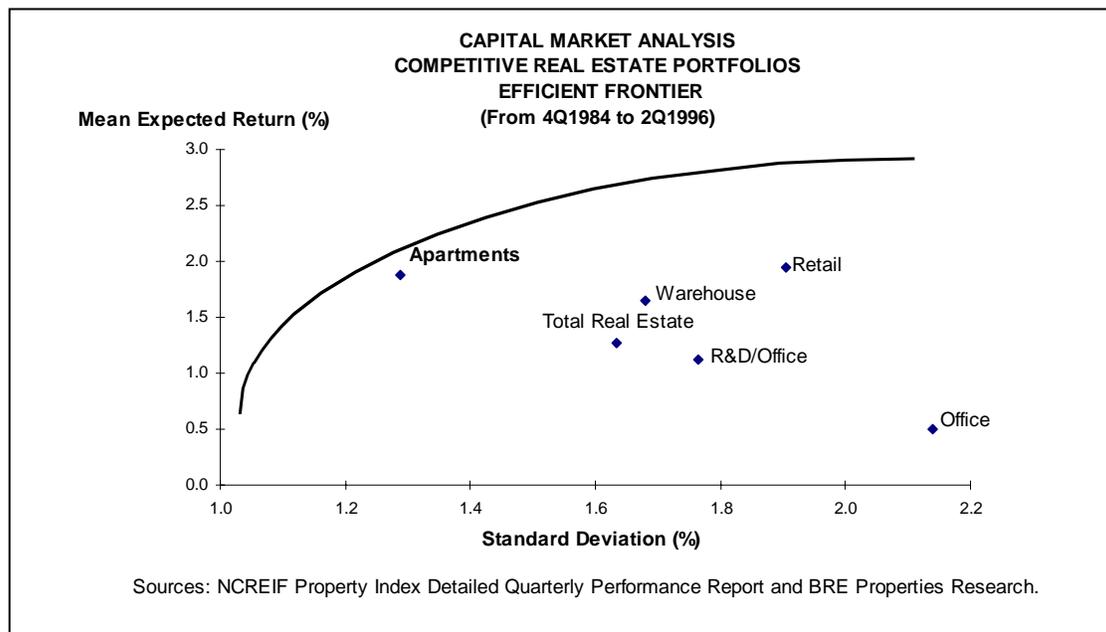
The apartment portfolio has exhibited high risk-adjusted returns compared to other real estate portfolios due to increased institutional interest, stable demand, and their ability to pass through inflationary increases, making them less volatile than other real estate assets.

The retail portfolio has provided high risk-adjusted returns over time due to growing consumer demand and effective buying income. The warehouse portfolio has provided high risk-adjusted returns due to the more stable nature derived by higher owner occupancy rates and shorter construction cycle, mitigating the risk of long oversupplied market conditions.

These real estate portfolios have also provided the highest return over time and will continue to attract large flows of institutional and speculative capital.

Contrarian or risk seeking investors will be attracted to the office and office/R&D sectors due to the probability of higher expected returns in the future, the belief that these sectors have reached their cyclical bottom and are moving into the recovery stage of their growth cycle.

These portfolios will start to attract large capital flows from institutional and speculative investors due to the perception that these assets are undervalued in comparison to other capital market assets.



COMPETITIVE REAL ESTATE PORTFOLIOS			
REAL ESTATE ASSET CLASS	STANDARD DEVIATION	MEAN EXPECTED RETURN	RETURN/RISK RATIO
<u>Risk Averse</u> Apartments	1.3	1.9	1.5
Retail	1.9	1.9	1.0
Warehouse	1.7	1.7	1.0
<u>Risk Neutral</u> Apartments	1.3	1.9	1.5
Retail	1.9	1.9	1.0
Warehouse	1.7	1.7	1.0
<u>Risky</u> Office	2.1	0.5	0.2
R&D/Office	1.8	1.1	0.6
Total Real Estate	1.6	1.3	0.8

Note: Please refer to the Appendix for the efficient frontier, risk-adjusted return table, total return graphs, and total return deviation graphs for more details.

Competitive Regional Real Estate Capital Markets Context

As illustrated in the table below, competitive regional real estate portfolios exhibiting the highest risk-adjusted returns are the Southeast, West North Central and Mideast.

These regional real estate portfolios have exhibited high risk-adjusted returns compared to other regional portfolios due to continued outmigration of population and businesses (capital flows) from the Northeast to the South and Mideast states.

Southeast states such as Tennessee (Knoxville/Memphis/Nashville), Mississippi (Birmingham), Alabama and Georgia (Atlanta); and Mideast states such as Maryland/Virginia (Washington D.C./Baltimore/Richmond), West Virginia (Charleston), North and South Carolina (Charlotte/Greensboro/Raleigh-Durham) and Kentucky (Lexington/Louisville).

West North Central states such as Minnesota, Iowa, Missouri, Kansas, Nebraska and North and South Dakota have experience some migration and institutional capital flows but at significantly lower levels seen in the Southeast and Mideast.

Slower migration and capital flows have kept the volatility of returns low and risk-adjusted returns high for this region. Due to stable migration and capital flow trends, real estate portfolios in this region should continue to provide the highest risk-adjusted returns over time and continue to attract additional institutional capital flows.

Risk neutral investors will continue to be attracted to the East Coast. Relatively high total expected returns along the East Coast are due to high population densities and effective buying income and the lack of developable land.

Contrarian or risk seeking investors will be attracted to the Southwest, Northeast, Mountain, Pacific and Western regions. The Southwest (Oklahoma, Arkansas, Louisiana and Texas) experienced low long-term risk-adjusted returns due largely to the oil and subsequent real estate busts of the mid-to-late 1980s.

The Northeast (Maine, New Hampshire, Vermont, Massachusetts, Rhode Island Connecticut, New York, New Jersey and Pennsylvania) has been adversely affected by continued outmigration of population and businesses (capital), high cost structures and slow economic growth.

The Mountain (Montana, Idaho, Wyoming Colorado, New Mexico, Arizona and Nevada) region is attractive to risk-averse and contrarian investors due to the level of total returns associated with higher risk. This region has attracted large flows of population and capital from the Pacific region.

This region should continue to be riskier, more sensitive to real estate boom-bust cycles, than other regions due to the momentum of capital inflows, population and employment growth and the abundance of developable land. This region will compensate investors for this additional risk through higher returns.

Contrarian and risk seeking investors will be attracted to the Pacific region (Washington, Oregon, California, Alaska and Hawaii). Low risk-adjusted returns for this region are associated with the severe regional recession experienced from 1992 through 1993, due largely to defense cutbacks.

The Pacific region's portfolio is expected to attract large capital flows from institutional and speculative investors due to the perception that these assets are undervalued in comparison to other capital market assets and that the regional economy is starting to recover.

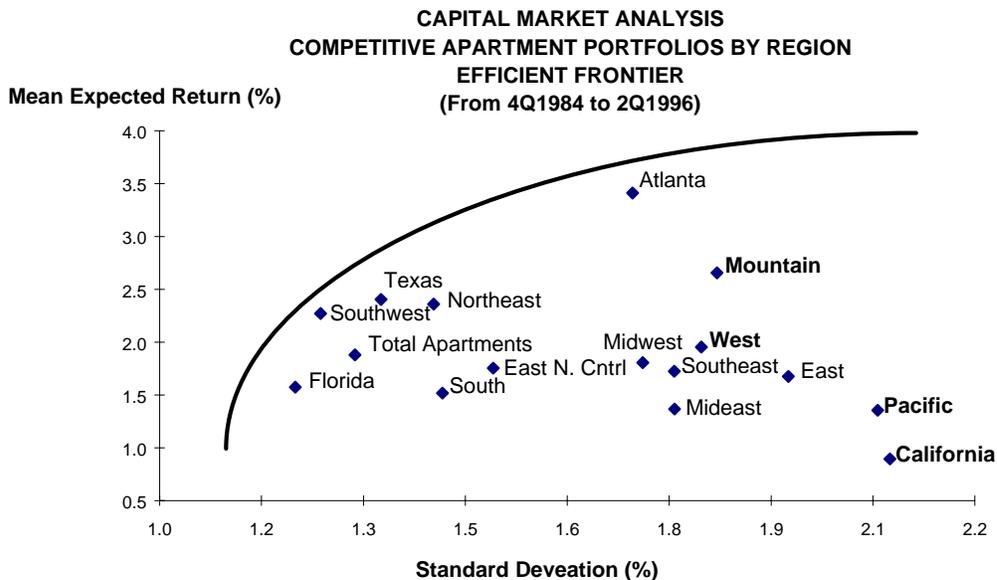
Apartments in a Competitive Regional Real Estate Capital Markets Context

As illustrated in the table below, competitive regional apartment portfolios exhibiting the highest risk-adjusted returns are the Southwest, Northeast and Mountain. Of the metro areas and states tracked, Atlanta and Texas rank the highest in risk-adjusted returns.

The Southwest apartment portfolio ranks high due to above average returns and low long term volatility. A significant portion of this portfolio is located in Texas. Texas has provided one of the highest risk-adjusted returns for apartments over time.

These Southwest and Mountain region apartment portfolios have exhibited high risk-adjusted returns compared to other regional apartment portfolios due to continued outmigration of population and businesses (capital flows) from the Northeast and Pacific regions. Total risk-adjusted returns remain high in the Northeast due to high population densities and effective income and lack of developable land. The migration of people and firms to the Mountain states should continue to provide this regional apartment portfolio with one of the highest risk-adjusted returns, therefore continuing to attract institutional capital flows.

Contrarian or risk seeking investors will be attracted to the Pacific (California) region due to the perception that these apartment portfolios are undervalued and have reached their real estate cycle bottom; and attracted to the Mideast due to high housing costs and population densities in the District of Columbia and rapid employment and population growth in North and South Carolina. For example, California's apartment portfolio is assumed to be slightly undervalued, the economy is in a recovery phase, new supply is limited and returns are not commensurate with the associated risk levels.



Source: NCREIF Property Index Detailed Quarterly Performance Report and BRE Properties Research.

COMPETITIVE APARTMENT PORTFOLIOS BY REGIONAL MARKETS			
MARKETS	STANDARD DEVIATION	MEAN EXPECTED RETURN	RETURN/RISK RATIO
<u>Risk Averse</u>			
Atlanta	1.7	3.4	2.0
Southwest	1.2	2.3	1.8
Texas	1.3	2.4	1.8
Northeast	1.4	2.4	1.7
Mountain	1.8	2.7	1.5
<u>Risk Neutral</u>			
Atlanta	1.7	3.4	2.0
Mountain	1.8	2.7	1.5
Texas	1.3	2.4	1.8
Northeast	1.4	2.4	1.7
Southeast	1.2	2.3	1.8
<u>Risky</u>			
California	2.1	0.9	0.4
Pacific	2.1	1.4	0.7
Mideast	1.8	1.4	0.7
East	1.9	1.7	0.9

Note: Please refer to the Appendix for the efficient frontier, risk-adjusted return table, total return graphs, and total return deviation graphs for more details.

Apartments in a Competitive Western Regional Real Estate Capital Markets Context

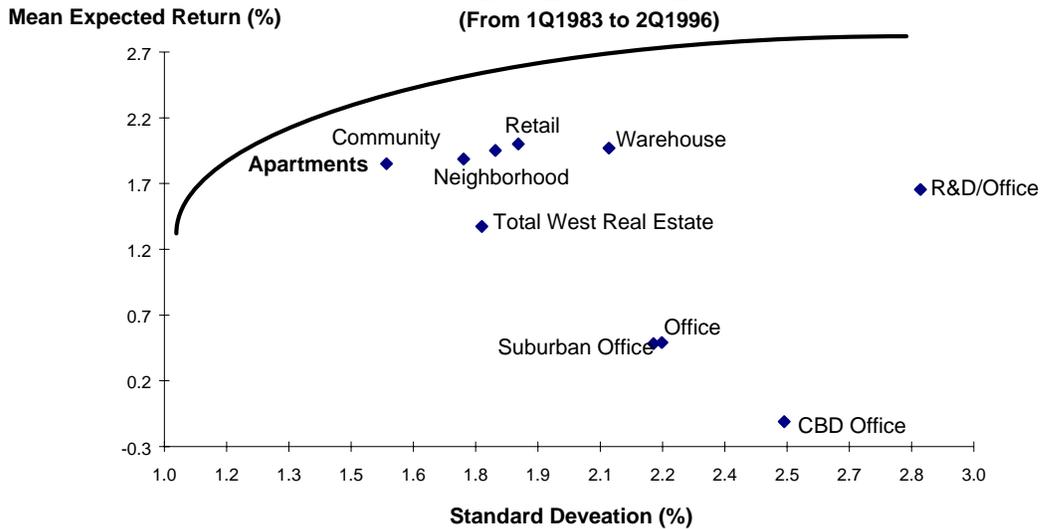
As illustrated in the table below, real estate portfolios in the Western region exhibiting the highest risk-adjusted returns are Neighborhood and Community Retail and Apartments.

These portfolios have exhibited lower levels of risk in comparison to other portfolios due to the more stable (demographic) nature of demand associated with these product types. Due to low volatility, these portfolios should continue to attract large flows of institutional capital.

Risk neutral investors will also be attracted to retail and apartment portfolios along with warehouse.

Contrarian or risk seeking investors will be attracted to CBD and Suburban Office portfolios. Demand for office space has driven vacancy rates down to their lowest level in over seven years. Office portfolios are considered to have reached their cyclical bottom and are considered undervalued compared to other capital market portfolios. With little new supply coming on-line, along with long construction cycles, large flows of speculative capital are expected for office product in the Western region.

**CAPITAL MARKET ANALYSIS
COMPETITIVE REAL ESTATE PORTFOLIOS IN THE WESTERN REGION
EFFICIENT FRONTIER
(From 1Q1983 to 2Q1996)**



Source: NCREIF Property Index Detailed Quarterly Performance Report and BRE Properties Research.

COMPETITIVE REAL ESTATE PORTFOLIOS IN THE WESTERN REGION			
REAL ESTATE ASSET CLASS	STANDARD DEVIATION	MEAN EXPECTED RETURN	RETURN/RISK RATIO
<u>Risk Averse</u>			
Neighborhood Retail	1.5	1.9	1.2
Community Retail	1.7	1.9	1.1
Apartments	1.8	2.0	1.1
<u>Risk Neutral</u>			
Retail	1.9	2.0	1.1
Warehouse	2.1	2.0	1.0
Apartments	1.8	2.0	1.1
<u>Risky</u>			
CBD Office	2.5	-0.1	0.0
Suburban Office	2.2	0.5	0.2
Office	2.2	0.5	0.2

Note: Please refer to the Appendix for the efficient frontier, risk-adjusted return table, total return graphs, and total return deviation graphs for more details.

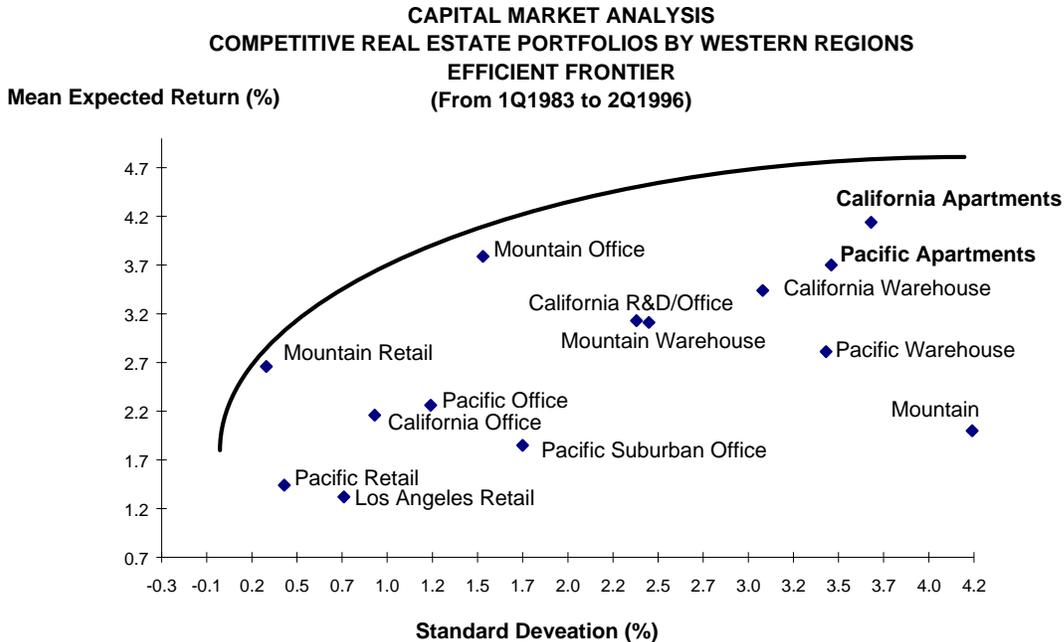
Apartments in a Competitive Western Sub-Regional Real Estate Capital Markets Context

As illustrated in the table below, real estate portfolios by Western regions with the highest risk-adjusted returns are Mountain and Pacific retail and Mountain office.

These portfolios have outperformed other competitive real estate portfolios amongst the Western regions due to high effective buying income in the Pacific region and high absolute demand, population and employment growth, in the Mountain region. Relatively low volatility along with above average expected returns will continue to attract large flows of institutional capital into Mountain retail and office and Pacific retail portfolios.

Risk neutral investors will continue to invest in California and Pacific apartments, and Mountain office, due to their high long-term expected returns.

High population/employment and capital flows into the Mountain region, coupled with high apartment supply, has made the apartment portfolio riskier, lowering its risk-adjusted return. Rising return volatility caused by the lingering affects of the California recession has significantly discounted the Pacific warehouse and apartment portfolios. Due to the perception that these portfolios are undervalued and that the Pacific region’s economy is recovering, these portfolios will attract large flows of speculative capital.



Source: NCREIF Property Index Detailed Quarterly Performance Report and BRE Properties

COMPETITIVE REAL ESTATE PORTFOLIOS BY WESTERN REGIONS			
REGION/REAL ESTATE ASSETS	STANDARD DEVIATION	MEAN EXPECTED RETURN	RETURN/RISK RATIO
<u>Risk Averse</u>			
Mountain Retail	0.3	2.7	9.5
Pacific Retail	0.4	1.4	3.8
Mountain Office	1.5	3.8	2.6
<u>Risk Neutral</u>			
California Apartments	3.6	4.1	1.1
Mountain Office	1.5	3.8	2.6
Pacific Apartments	3.4	3.7	1.1
<u>Risky</u>			
Mountain Apartments	4.2	2.0	0.5
Pacific Warehouse	3.4	2.8	0.8
Pacific Apartments	3.4	3.7	1.1

Note: Please refer to the Appendix for the efficient frontier, risk-adjusted return table, total return graphs, and total return deviation graphs for more details.

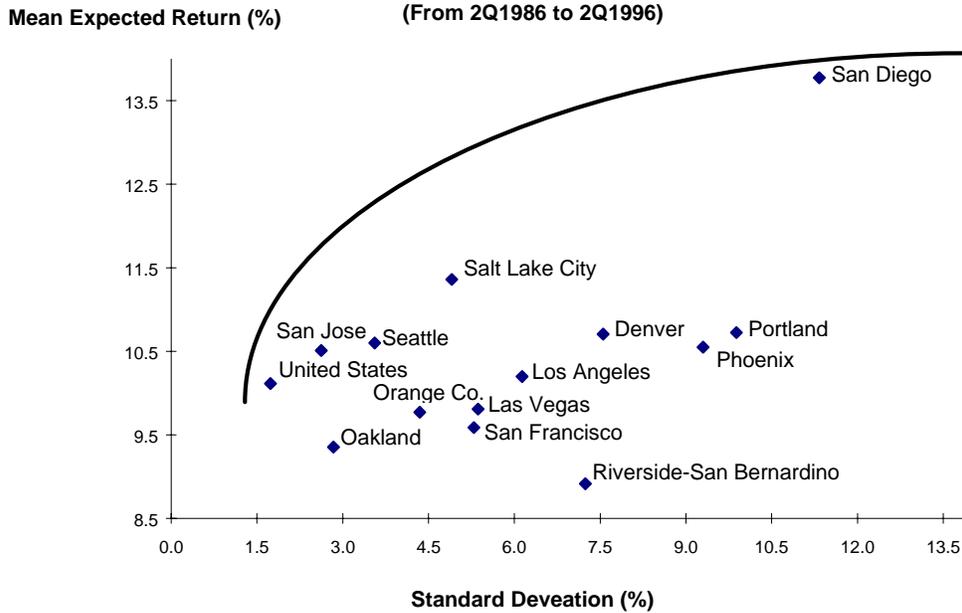
Apartments in a Competitive Western Regional-Metro Area Real Estate Capital Markets Context

As illustrated in the table below, metro area apartment portfolios in the Western region with the highest risk-adjusted returns are San Jose, Oakland and Seattle.

These portfolios have exhibited the highest risk-adjusted rates of return over time because of their infill nature, high population densities and healthy employment growth. Due to equilibrium conditions in Portland and Phoenix and the severity of the economic downturn in San Diego, these portfolios have been heavily discounted.

Due to the lack of new supply and stable nature of the San Jose, Oakland and Seattle apartment portfolios, large flows of institutional capital should continue. Speculative capital will flow to Portland and Phoenix as long as their is healthy population/employment growth and availability of developable land. These markets have a higher potential for overbuilding, therefore higher return volatility, in the short-run. San Diego will attract both risk-averse and speculative capital flows due to the expectation of future higher economic growth, low supply and high expected returns.

**CAPITAL MARKET ANALYSIS
COMPETITIVE METROPOLITAN APARTMENT PORTFOLIOS IN THE WESTERN REGION
EFFICIENT FRONTIER**



Source: The National Real Estate Index and BRE Properties Research Department.

COMPETITIVE METRO AREA APARTMENT PORTFOLIOS IN THE WESTERN REGION			
MARKETS	STANDARD DEVIATION	MEAN EXPECTED RETURN	RETURN/RISK RATIO
<u>Risk Averse</u>			
San Jose	2.6	10.5	4.0
Oakland	2.8	9.4	3.3
Seattle	3.6	10.6	3.0
<u>Risk Neutral</u>			
San Diego	11.3	13.8	1.2
Seattle	3.6	10.6	3.0
Portland	9.9	10.7	1.1
<u>Risky</u>			
Portland	9.9	10.7	1.1
Phoenix	9.3	10.5	1.1
San Diego	11.3	13.8	1.2

Note: Please refer to the Appendix for the efficient frontier, risk-adjusted return table, total return graphs, and total return deviation graphs for more details.

Apartment REITs in a Competitive Real Estate Capital Markets Context

As illustrated in the table below, REIT portfolios exhibiting the highest risk-adjusted returns are Bay Apartments, Colonial Properties Trust, Post Properties and BRE Properties.

- Bay Apartments ranks first due to large capital inflows and high returns from their concentration in Bay Area apartment properties and development capabilities.
- Colonial Properties ranks high due to its management capabilities, Southern focus and recovery in the office sector.
- Post Properties ranks high due to its operational efficiencies, management capabilities, Southern focus and high historical risk-adjusted returns generated from its Atlanta properties.
- BRE Properties ranks high due to its management capabilities, Western regional focus and high returns generated from its Pacific Northwest and Bay Area properties.

These portfolios have exhibited high risk-adjusted returns in comparison to other REITs due to their property focus, management capabilities and increased interest in apartments by institutional investors. Due to their ability to rapidly pass-through inflationary increases, provide stable returns (low volatility) over time and are underweighted in most institutional portfolios, the apartment REIT portfolio should continue to attract large flows of institutional capital.

Risk neutral investors will continue to be attracted to Merry Land, Bay Apartments, Security Capital and BRE Properties due to their high expected rates of return.

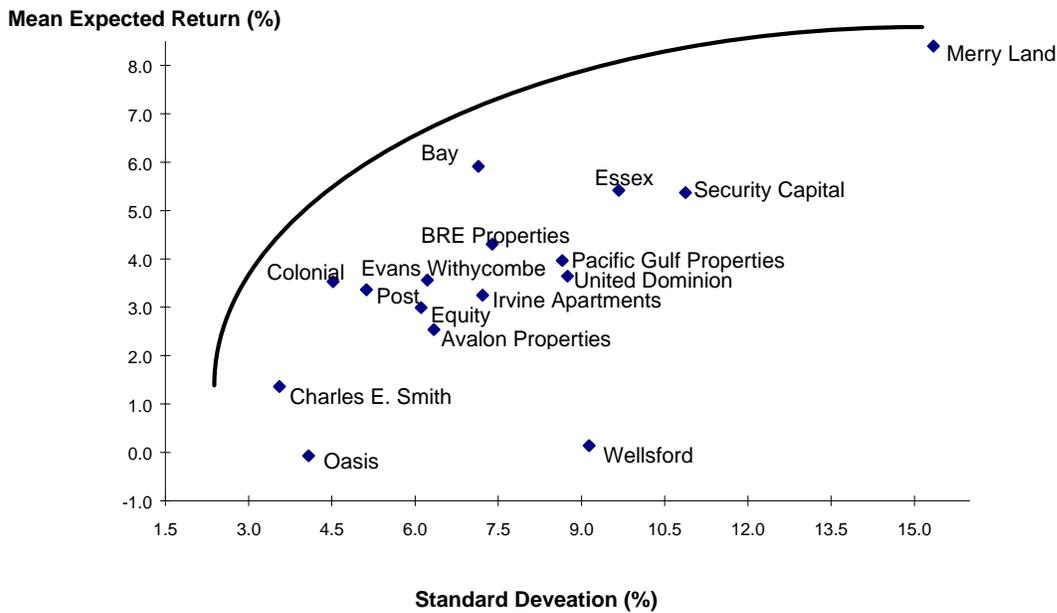
REIT portfolios exhibiting the lowest risk-adjusted returns are Oasis Properties, Wellsford Residential, Charles E. Smith and Avalon Properties.

Low risk-adjusted returns for:

- Oasis Properties is due to its over concentration in the highly volatile Las Vegas apartment market, high institutional ownership and some controversies concerning top management.
- Wellsford Residential is due to slow management integration after the merger, high debt and problems associated with restructuring their balance sheet, and portfolio concentrations in markets such as Tucson, Phoenix, Dallas, San Antonio and Seattle-Tacoma.
- Charles E. Smith due to high debt, large institutional and insider ownership, and portfolio concentrations in older infill locations in the Washington D.C. metro area.
- Avalon Properties due to their portfolio concentration in the Northeast and high institutional ownership.

These portfolios will continue to attract more speculative capital flows.

**CAPITAL MARKET ANALYSIS
COMPETITIVE APARTMENT REIT PORTFOLIOS
EFFICIENT FRONTIER**



Source: Dean Witter Reynolds Investment Banking and and BRE Properties Research.

COMPETITIVE APARTMENT REIT PORTFOLIOS			
REITS	STANDARD DEVIATION	MEAN EXPECTED RETURN	RETURN/RISK RATIO
<u>Risk Averse</u>			
Bay Apartments	7.1	5.9	0.8
Colonial Properties Trust	4.5	3.5	0.8
Post Properties	5.1	3.4	0.7
BRE Properties	7.4	4.3	0.6
<u>Risk Neutral</u>			
Merry Land	15.34	8.4	0.6
Bay Apartments	7.1	5.9	0.8
Security Capital	10.9	5.4	0.5
BRE Properties	7.4	4.3	0.6
<u>Risky</u>			
Oasis Properties	4.1	-0.1	-0.1
Wellsford Residential	9.1	0.1	0.0
Charles E. Smith	3.6	1.4	0.4
Avalon Properties	6.3	2.5	0.4

Note: Please refer to the Appendix for the efficient frontier, risk-adjusted return table, total return graphs, and total return deviation graphs for more details.

Conclusions and Recommendations

Summary of Results

- Capital market portfolios exhibiting the highest risk-adjusted returns are T-Bills, Inflation and Apartments.
- Real estate portfolios exhibiting the highest risk-adjusted returns are apartments, retail and warehouse.
- Competitive regional real estate portfolios exhibiting the highest risk-adjusted returns are the Southeast, West North Central and Mideast.
- Competitive regional apartment portfolios exhibiting the highest risk-adjusted returns are the Southwest, Northeast and Mountain.
- Real estate portfolios in the Western region exhibiting the highest risk-adjusted returns are Neighborhood and Community Retail and Apartments.
- Real estate portfolios by Western regions with the highest risk-adjusted returns are Mountain and Pacific Retail and Mountain Office.
- Metro area apartment portfolios in the Western region with the highest risk-adjusted returns are San Jose, Oakland and Seattle.
- REIT portfolios exhibiting the highest risk-adjusted returns are Bay Apartments, Colonial Properties Trust, Post Properties and BRE Properties.

Summary Conclusions and Recommendations

- Risk-averse institutional investors should continue to invest in portfolios and asset classes that give them the highest long term risk adjusted rates of returns: Mountain and Pacific regions and apartment portfolios in metro areas located in the Bay Area and Seattle.
- Risk-neutral investors should continue to invest in portfolios and asset classes that give them the highest long term expected rates of returns: metro areas located in the Pacific, Pacific Northwest and Mountain regions.
- Contrarian, speculative or risk-seeking investors should invest in portfolios and asset classes that give them the opportunity to obtain high abnormal rates of returns: office portfolios in the West and apartment portfolios in the Pacific region.

Conclusions

Assuming the majority of investors are risk-averse and capital flows freely across markets, institutional capital flows will continue to be attracted to investments offering the highest risk-adjusted rates of return. From this study, portfolios offering the highest risk-adjusted rates of return are:

COMPETITIVE CAPITAL MARKET PORTFOLIOS			
ASSET CLASS	STANDARD DEVIATION	MEAN EXPECTED RETURN	RETURN/RISK RATIO
Risk Averse			
<i>Mountain Retail</i>	0.3	2.7	9.5
San Jose Apartments	2.6	10.5	4.0
<i>Pacific Retail</i>	0.4	1.4	3.8
91 Day T-Bills	0.4	1.4	3.5
Oakland Apartments	2.8	9.4	3.3
Seattle Apartments	3.6	10.6	3.0
<i>Mountain Office</i>	1.5	3.8	2.6
Atlanta Apartments	1.7	3.4	2.0
Inflation (CPI)	0.5	0.9	1.8
Southwest Apartments	1.2	2.3	1.8
Texas Apartments	1.3	2.4	1.8
Northeast Apartments	1.4	2.4	1.7
Mountain Apartments	1.8	2.7	1.5
Apartments	1.3	1.9	1.5
<i>West Neighborhood Retail</i>	1.5	1.9	1.2
<i>West Community Retail</i>	1.7	1.9	1.1
West Apartments	1.8	2.0	1.1
Southeast	1.6	1.8	1.1
West North Central	1.4	1.5	1.1
Retail	1.9	1.9	1.0
Warehouse	1.7	1.7	1.0
Mideast	1.8	1.8	1.0

Due to their relatively high risk-adjusted rates of return compared to other capital market assets, these portfolios will continue to absorb the majority of risk-averse institutional capital allocations.

Investors willing to take the risk or are risk neutral will search the capital markets for the highest expected return. From this study, portfolios offering the highest expected rates of return are:

COMPETITIVE CAPITAL MARKET PORTFOLIOS			
ASSET CLASS	STANDARD DEVIATION	MEAN EXPECTED RETURN	RETURN/RISK RATIO
Risk Neutral			
San Diego Apartments	11.3	13.8	1.2
Seattle Apartments	3.6	10.6	3.0
Portland Apartments	9.9	10.7	1.1
California Apartments	3.6	4.1	1.1
S&P 500	7.2	4.1	0.6
<i>Mountain Office</i>	<i>1.5</i>	<i>3.8</i>	<i>2.6</i>
Pacific Apartments	3.4	3.7	1.1
Atlanta Apartments	1.7	3.4	2.0
REITs	6.5	2.9	0.4
Mountain Apartments	1.8	2.7	1.5
Gov./Corp.Bonds	2.9	2.5	0.8
Texas Apartments	1.3	2.4	1.8
Northeast Apartments	1.4	2.4	1.7
Southeast Apartments	1.2	2.3	1.8
West Retail	1.9	2.0	1.1
West Warehouse	2.1	2.0	1.0
West Apartments	1.8	2.0	1.1
Apartments	1.3	1.9	1.5
Retail	1.9	1.9	1.0
East North Central	2.2	1.8	0.8
East	2.3	1.8	0.8
Southeast	1.6	1.8	1.1
Warehouse	1.7	1.7	1.0

Due to their relatively high rates of return compared to other capital market assets, these portfolios will continue to absorb a significant amount of risk-averse and speculative capital allocations.

Assuming that capital markets are efficient and eventually clear at the market equilibrium price, investors demand to be compensated for taking risk, market and asset values are cyclical, and capital flows freely across markets, speculators and risk seekers will continue to search the capital markets for arbitrage opportunities. These investors will be attracted to investments offering the lowest risk-adjusted rates of return in anticipation of the possibility of achieving abnormal rates of return in the future. From this study, portfolios offering the lowest risk-adjusted rates of return are:

COMPETITIVE CAPITAL MARKET PORTFOLIOS			
ASSET CLASS	STANDARD DEVIATION	MEAN EXPECTED RETURN	RETURN/RISK RATIO
Risk Seeker			
<i>West CBD Office</i>	2.5	-0.1	0.0
<i>West Suburban Office</i>	2.2	0.5	0.2
<i>West Office</i>	2.2	0.5	0.2
Office	2.1	0.5	0.2
Southwest	1.7	0.7	0.4
California Apartments	2.1	0.9	0.4
REITs	6.5	2.9	0.4
Mountain Apartments	4.2	2.0	0.5
S&P500	7.2	4.1	0.6
R&D/Office	1.8	1.1	0.6
Northeast	2.6	1.7	0.7
Mountain	1.7	1.2	0.7
Pacific Apartments	2.1	1.4	0.7
Mideast Apartments	1.8	1.4	0.7
<i>Pacific Warehouse</i>	3.4	2.8	0.8
Gov.Oblig. Bonds	3.0	2.3	0.8
Total Real Estate	1.6	1.3	0.8
Pacific	1.9	1.4	0.8
West	1.8	1.4	0.8
East Apartments	1.9	1.7	0.9
Pacific Apartments	3.4	3.7	1.1
Portland Apartments	9.9	10.7	1.1
Phoenix Apartments	9.3	10.5	1.1
San Diego Apartments	11.3	13.8	1.2

Due to their relatively low risk-adjusted rates of return compared to other capital market assets, these portfolios will attract contrarian, speculative and risk-seeking capital flows.

Recommendations

Risk-averse institutional investors should continue to invest in portfolios and asset classes that give them the highest long term risk adjusted rates of returns. Capital market portfolios offering the highest risk-adjusted rates of return are retail portfolios in the Mountain and Pacific regions and apartment portfolios in metro areas located in the Bay Area and Seattle.

Risk-neutral investors should continue to invest in portfolios and asset classes that give them the highest long term expected rates of returns. Capital market portfolios offering the highest expected rates of return are apartment portfolios, especially metro areas located in the Pacific, Pacific Northwest and Mountain regions.

Contrarian, speculative or risk-seeking investors should invest in portfolios and asset classes that give them the opportunity to obtain high abnormal rates of returns. Capital market portfolios offering the lowest risk-adjusted rates of return are office portfolios in the West and apartment portfolios in the Pacific region. These portfolios could be considered oversold, have reached their cyclical bottom and are poised for higher expected rates of return in the future.

Research Criticisms

Appraisal Based Return Data

- Returns Base on Appraisals not Action Market
- Appraisal Smoothing (More Write ups than Write downs)
- Nonnormality of Data (Skewness/Bias)
- Short Sample Periods (Large Sampling Error)

Real Estate Market Efficiency

- Illiquidity
- High transaction costs (Market Friction)
- High information costs
- Information Lags

Future Research

Recommendations for future research are to continue to develop portfolio strategies based on regression analysis, correlation analysis, and geographic, economic base and time diversification analysis; and to develop a strategy to construct an optimal portfolio allocation strategy based on the highest risk adjusted expected rate of return for target markets.

RESEARCH DESIGN II

PORTFOLIO DIVERSIFICATION AND OPTIMIZATION PROGRAM

Introduction

The goal of this research project is to identify the optimal portfolio weights by geographic region for an existing and future apartment REIT apartment portfolio. The REIT's current strategy is to acquire and develop in 14 metropolitan areas within the western region.

<i>Coastal Markets</i>	<i>Desert Markets</i>	<i>Mountain Markets</i>
<i>Los Angeles-Ventura</i>	<i>Las Vegas</i>	<i>Albuquerque</i>
<i>Orange County</i>	<i>Phoenix</i>	<i>Denver</i>
<i>Portland</i>	<i>Tucson</i>	<i>Salt Lake</i>
<i>Riverside-San Bernardino</i>		
<i>Sacramento</i>		
<i>San Diego</i>		
<i>San Francisco Bay Area</i>		
<i>Seattle</i>		

The mission of this research is to identify the optimal portfolio mix based on economic, demographic, and apartment market indicators.

Portfolio Diversification

The first phase of the portfolio optimization project is to measure the correlation between economic variables and apartment returns within the 14 target markets. The goal of these tests is to determine the degree to which economic or demographic variables help explain movements in apartment returns. Since apartment return data is limited, running these tests on the data that is available allows us to identify economic variables that are statistically significant in their predictability of future apartment returns.

By using economic variables produced by government agencies and collected in and on a consistent basis, we can go back as far as the late 1970s, compared to the late 1980s for apartment return data. The ability to go back to the late 1970s allows us to assemble a large sample data set. Under statistical theory, if the sample size is significantly large, it will approximate a normal (bell curve) distribution. The normality of the data is a prerequisite for using mean-variance analysis or modern (Markowitz) portfolio optimization techniques.

Portfolio Optimization

The second phase of the portfolio diversification study is to identify optimal portfolio allocations that achieve the highest expected rate of return at the lowest level of risk for the portfolio. This phase determines the optimal portfolio weighting by geographic area. The goal of this phase is to compare the REIT's portfolio diversification to a risk-return weighted ("target") portfolio, then, from the variances, optimal vs. actual allocations, a recommended acquisition strategy is structured to eliminate, to the extent possible, the risk of excess geographic concentration in the portfolio.

Variable Determination

Economic theory

Based on regional and urban economic theory, literature research and consultation with economists, economic variables with the highest probability for predicting total apartment returns by metro area over time are identified. These economic variables were tested against a limited series of actual return data by metro for validation of their statistical significance.

After reviewing the literature, an inventory of supply and demand data factors were compiled. After running the correlation analysis, and lagged time period correlation analysis, the following factors are considered significant in predicting future housing supply and demand.

Supply Factors

Factors showing strong correlation with housing supply are:

- Single and multi-family housing starts (0 periods)
- CPI growth (-9 periods)
- Consumer confidence (-1 periods)
- Absolute change in GDP (0 periods)
- Change in home prices (-5 periods)
- Change in housing inventory (-4 periods)
- Interest Rates (0 periods)
- Affordability (0 periods)

Demand Variables	Correlation Coef.	t Stats
YOY Ann. Absolute Change GDP (0)	52.59%	6.57
YOY Ann. Absol.Change Housing Inventory (-4)	42.38%	4.97
Rolling Ann.Qtr. Avg.10 year Int. Rts.(0)	28.56%	-3.17
YOY Ann. % Change Personal Income Per Household (-3)	47.98%	5.81
Rolling Ann.Qtr. Avg.Housing Affordability Index (0)	28.17%	3.07
YOY Ann. % Change CPI Ndx. (-9)	57.50%	7.47
YOY Ann. % Change Home Price (-5)	49.91%	6.12
YOY Ann. % Change Consumer Confidence Index (-1)	57.39%	6.49
Rolling Ann.Qtr. Avg.Home Sales (0)	2.47%	0.26
Rolling Ann.Qtr. Avg.Single-Family Starts (0)	79.40%	13.88
Rolling Ann.Qtr. Avg.Multifamily Starts (0)	84.84%	17.04

Note: Numbers in parentheses are the number of lagged periods.

Demand Factors

Factors showing strong correlation with housing demand are:

- Number of persons per household (0 periods)
- Home price appreciation (0 periods)
- Income per household growth (-2 periods)
- Inflation rate (0 periods)
- Employment growth (-1 periods)

Demand Variables	Correlation Coef.	t Stats
YOY Ann. Absolute Change GDP (0)	15.70%	1.69
YOY Ann. Change EMPLOY (-1)	21.50%	2.33
Rolling Ann.Qtr. Avg.UNEMP (-1)	17.63%	-1.91
YOY Ann. Change POP24-65 (0)	10.10%	1.07
Number of Persons Per Hhld. (0)	61.70%	8.33
YOY Ann. % Change Personal Income Per Household (-2)	51.90%	6.45
Rolling Ann.Qtr. Avg.Housing Affordability Index (-0)	22.53%	2.41
YOY Ann. % Change Home Price (0)	57.01%	7.37
Rolling Ann.Qtr. Avg.10 year Int. Rts.(0)	13.75%	-1.47
YOY Ann. % Change CPI Ndx. (0)	28.09%	3.11

Reduced Form - Supply Model Forecast Equation

Of the significant supply variables, change in GDP (IVGDP), change in housing inventory (HOUSINGINV) lagged four periods, mortgage interest rates (IVINTRT) and inflation (IVCPI) lagged nine periods produced a statistically significant forecast model and adheres to economic theory. This model is used to forecast future housing supply (starts).

$$\begin{aligned} \text{DVSTARTS} = & 975,792 + 1.44 (\text{IVGDP}(0)) + 0.11 (\text{HOUSINGINV}(-4)) + \\ & \qquad \qquad \qquad [8.16] \qquad \qquad \qquad [4.06] \\ & -14,269 (\text{IVINTRT}(0)) + 5,528,833 (\text{IVCPI}(-9)) \\ & \qquad \qquad \qquad [-1.53] \qquad \qquad \qquad [8.86] \end{aligned}$$

Multiple R = 82% R Square = 67% Adj. R Square = 66% F Stat = 55.7

Reduced Form - Demand Model Forecast Equation

Of the significant demand variables, change in GDP (IVGDP), change in number of persons per household (IVPERSPERHHLD), and home sales price appreciation (IVSAL\$GTH) produced a statistically significant forecast model and adheres to economic theory. This model is used to forecast future housing demand (household formations).

$$\begin{aligned} \text{DVHHLDS} = & -2,923,272 + 1.05 (\text{IVGDP}(0)) + 1,374,827 (\text{IVPERSPERHHLD}(0)) + \\ & \qquad \qquad \qquad [4.70] \qquad \qquad \qquad [6.86] \\ & 3,654,143 (\text{IVSAL$GTH}(0)) \\ & \qquad \qquad \qquad [-1.53] \end{aligned}$$

Multiple R = 75% R Square = 56% Adj. R Square = 55% F Stat = 46.9

Note: Numbers in brackets are “t” statistics; and numbers in parentheses are number of lagged periods. Regression was run at a 90% confidence level.

Parameter Production and Data Manipulation

Economic and Market Variables

Economic variables used in this analysis were taken from the National Real Estate Index and from Regional Financial Associates economic and demographic databases.

Apartment Returns

The Koll/National Real Estate Index (NREI) is a biannual/quarterly survey based on a sample of apartment sales within each metro area over time. Total returns were derived by adding together the biannual/quarterly percentage change in sales price per square foot with the biannual/quarterly capitalization rate to arrive at a total return figure. Total apartment returns were calculated for 14 target markets on a biannual/quarterly basis from 1986 through to the first quarter of 1998.

TOTAL APARTMENT RETURNS = INCOME RETURN + CAPITAL APPRECIATION

$$= \frac{\text{NET OPERATING INCOME}}{\text{SALES PRICE}} + \frac{\text{PRICE}_{t+1} - \text{PRICE}_t}{\text{PRICE}_t}$$

Note: Year-Over-Year total apartment returns were calculate on a quarterly basis to maximize the time series sample size.

Economic Variables

Market equilibrium and supply/demand ratios, and year-over-year absolute and percent changes, were calculated for 14 target markets on and biannual/quarterly basis from 1979 through to the first quarter of 1998. Economic variables used for this analysis include:

<i>Demand Drivers</i>	<i>Supply Components</i>	<i>Supply/Demand Measures</i>
<ul style="list-style-type: none"> ▪ <i>Total Non-Farm Employment</i> ▪ <i>Nominal Gross Domestic Product²</i> ▪ <i>Total Population</i> ▪ <i>Population Between 25-44 Years Old</i> ▪ <i>Total Households</i> 	<ul style="list-style-type: none"> ▪ <i>Total Residential Permits</i> ▪ <i>Total Multifamily Permits</i> ▪ <i>Ratio of Total Multifamily Permits to Total Residential Permits</i> 	<ul style="list-style-type: none"> ▪ <i>Ratio of Total Residential Permits to Household Formations</i> ▪ <i>Housing Affordability</i> ▪ <i>Median Home Prices</i> ▪ <i>Total Housing Returns</i>

¹ Beginning the data series in 1979 incorporates random economic and political events and business cycles including the recessions of the early-to-mid '80's and '90-'91 and the recoveries of '86-89 and '93-'98.

² Employment demand driver.

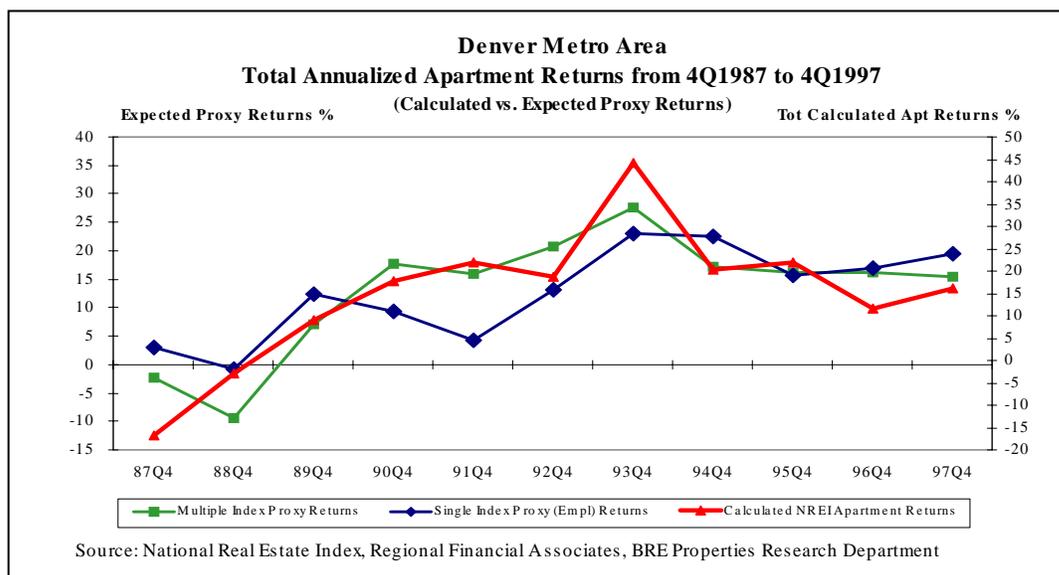
Time Series Analysis

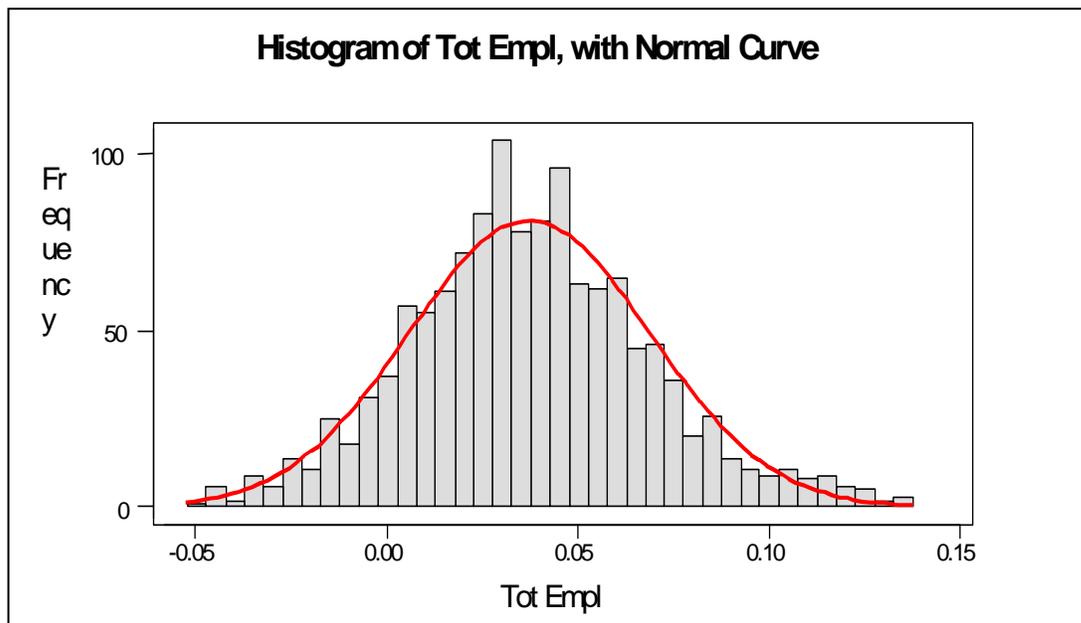
Prior to building the model we need to know how far back in time we should go with the data. We did not want to be going back too far, especially into the '70s, because you had monetary shocks, hyperinflation, stagflation and the Vietnam War. These exogenous and endogenous shocks created distortions in the economy at that time. The real stable state in the economy started in 1979 and has continued through to 1998.

By going back to 1979 we were still able to incorporate other important random economic and political events and business cycles, you want to have these events in your time series. For this time period we have both recessions of the early-to-mid 1980's, a full recovery period from 1986 to 1989, the recession of 1990 and 1991, and the recovery period up to 1998. From this standpoint, we feel confident that we have a large enough sample of data to be able to generate a normal distribution.

Graphing Data

Before one embarks on a statistical analysis the data needs to be graphed to identify its characteristics. The first series of graphs plots the dependent and independent variable on one x-y plot. This allows for quick identification of the relationship between the two series. The second set of graphs plots the data set or sample as a histogram to see if it normally distributed. If the data set is normally distributed then we can use mean-variance analysis or the Markowitz optimization methodology.





Properties of a normally distributed data set are: 1) The normal distribution curve is symmetrical around its mean value, 2) the probability of obtaining a value of a normally distributed random variable far away from its mean becomes progressively smaller, and 3) a linear combination of two or more normally distributed random variables is itself normally distributed, which means there is a high degree of predictability of returns in the regression model.

When the histograms approximate a normal distribution, we can assume our data set is large enough and homogeneous enough to produce reliable statistical results. Once the data has been graphed, regression and correlation analysis is conducted to test for statistical significance in the relationship between total apartment returns and economic and demographic data. If the data are significant in the relationship to total apartment returns—*then we can use the economic and/or demographic data as a proxy for expected apartment returns.*

Testing of the Market Model

Regression and correlation analysis allows us to test whether a relationship exists between two variables. These methods provide the bases for estimating the values of one variable from known or assumed values of one or more other variables and for measuring the strength of the relationships among the variables.

Model Types

Using a single index regression model allows us to make estimates of apartment returns from knowledge of the values of one other variable, employment for example, and to the measurement of the errors involved in this analysis. The multiple regression model is an extension of the single index model where two or more independent variables, employment and permits for example, are used to estimate the values for total apartment returns by metro area.

Testing Relationships Between Apartment Returns and Economic Variables

To test the relationship between two variables we use the single index regression model and correlation analysis. Correlation Coefficient is a measure of linear association between two variables. If correlations among the variables are high then there is the possibility that very high similarity among the variables exists.

Other tests for relational significance are R^2 , F test, t test, Durbin-Watson statistic and P values. These measures of statistical significance are discussed in the Glossary.

When using a multiple index regression model we must be careful to test the structure of the model. Troubleshooting the multiple index regression model is discussed in the Appendix.

Methodology

Single Index Model

The first phase of the analysis is to evaluate the influence of basic demand on apartment returns, since we do not have complete apartment return statistics that have been collected consistently over a long period of time. What we do have is calculated return statistics from the National Real Estate Index going back to 1985 on a quarterly basis.

To make up for this deficiency we need to identify economic and/or demographic variables that help to explain movements in the total apartment return data we do have, then use these variables as proxies for total apartment returns for each given metro area.

To determine proxy returns we run regressions using economic variables such as employment, population, household GDP, the population cohort between 18 and 44, change in home prices, etc. against NREI total apartment returns. This is a single index model approach to screen all the economic and demographic variables for statistical significance. From the screening process we came up with employment as the most statistically significant variable that helps to explain total returns provided by the National Real Estate Index for our 14 target markets.

This result allows us to create a proxy for total apartment returns using employment growth as the proxy. Since the total return statistics from the National Real Estate Index only go back to 1985, we can now go even further back in time, another ten years, enabling us to get a large enough sample size that approximates a normal distribution. Now we can use the Markowitz mean-variance optimization approach to determine the optimal portfolio weights.

Multiple Index Model

Using the single index regression model is useful in screening variables for statistical significance, but the single index model is limited in its ability to explain total apartment returns, employment is only one variable on the demand that helps explain total apartment returns, it does not take into consideration supply side variables. To arrive at a better predictor for apartment returns, a multiple index model is developed with supply and demand variables generating more accurate expected proxy returns.

After we test the single index model with variables such as employment, population and household, etc., looking for specific economic indicators that will help predict apartment returns at the metro level, we can then develop a multiple regression model. This model is more theoretically sound because it includes variables such as housing affordability, permits to households ratio, and the age cohorts of renters, along with employment. Ideally this model should be restricted to no more than five independent variables.

Once the variables have been identified, we can then test combinations to determine the best model for predicting apartment returns. Once you have run the regressions you check to see if the variable statistics are significant by using what are called “t” and “F” statistics, the rule of thumb is that the “t” should be greater than two and the “F” greater than four.

Multiple Regression Results

Ordinary Least Squares (OLS) Multiple Regression Results – Reduced Form

After eliminating redundant variables to reduce multicollinearity, and variables with low single-linear regression statistics, 14 linear regression models were developed, one for each metro area.

The significant variables detected, total change in employment (EMP), change in employment between the ages of 24 years old to 44 years old (POP2544), change in multifamily permits (MFPERM), and single-family housing affordability (AFFIDX) produced the most statistically significant model across all metro areas, and adheres to real estate housing economic theory. This model will be used as the primary forecast tool to determine future expected returns for metro area apartment markets. These return projections along with covariances will be use for active portfolio optimization procedures.

Los Angeles

$$\begin{aligned} \text{APT RETURN} &= 14.86 + 3.7680 (\text{EMP}) - 2.8684 (\text{POP2544}) - 0.0169 (\text{MFPERM}) \\ &\quad [4.68] \qquad \qquad \qquad [-2.51] \qquad \qquad \qquad [-0.59] \\ &\quad - 0.0682 (\text{AFFIDX}) \\ &\quad \qquad \qquad \qquad \qquad \qquad \qquad [-0.37] \end{aligned}$$

Durbin-Watson = 80% R-Square = 61% Adj. R Square = 56% F Stat = 11.54

Orange County

$$\begin{aligned} \text{APT RETURN} &= 11.52 + 2.0819 (\text{EMP}) - 1.3303 (\text{POP2544}) - 0.0079 (\text{MFPERM}) \\ &\quad [3.87] \qquad \qquad \qquad [-1.28] \qquad \qquad \qquad [-1.03] \\ &\quad - 0.3160 (\text{AFFIDX}) \\ &\quad \qquad \qquad \qquad \qquad \qquad \qquad [-2.34] \end{aligned}$$

Durbin-Watson = 88% R-Square = 65% Adj. R Square = 60% F Stat = 13.40

Inland Empire

$$\begin{aligned} \text{APT RETURN} &= 6.102 + 2.9621 (\text{EMP}) - 1.6415 (\text{POP2544}) + 0.0169 (\text{MFPERM}) \\ &\quad [1.89] \qquad \qquad \qquad [-1.41] \qquad \qquad \qquad [+1.29] \\ &\quad - 0.0815 (\text{AFFIDX}) \\ &\quad \qquad \qquad \qquad \qquad \qquad \qquad [-0.19] \end{aligned}$$

Durbin-Watson = 67% R-Square = 20% Adj. R Square = 09% F Stat = 1.83

San Diego

$$\begin{aligned} \text{APT RETURN} &= 10.72 + 2.2956 (\text{EMP}) - 1.7594 (\text{POP2544}) + 0.0333 (\text{MFPERM}) \\ &\quad [2.61] \qquad \qquad \qquad [-2.04] \qquad \qquad \qquad [+2.77] \\ &\quad - 0.3426 (\text{AFFIDX}) \\ &\quad \qquad \qquad \qquad \qquad \qquad \qquad [-1.77] \end{aligned}$$

Durbin-Watson = 123% R-Square = 63% Adj. R Square = 58% F Stat = 15.57

San Francisco Bay Area

$$\begin{aligned} \text{APT RETURN} &= 10.01 + 3.4287 (\text{EMP}) + 3.4285 (\text{POP2544}) + 0.0447 (\text{MFPERM}) \\ &\quad [4.21] \quad \quad \quad [+1.80] \quad \quad \quad [+2.35] \\ &\quad - 0.0928 (\text{AFFIDX}) \\ &\quad \quad \quad [-0.42] \end{aligned}$$

Durbin-Watson = 89% R-Square = 83% Adj. R Square = 80% F Stat = 26.86

Sacramento

$$\begin{aligned} \text{APT RETURN} &= 05.78 + 3.0960 (\text{EMP}) - 0.5749 (\text{POP2544}) + 0.0017 (\text{MFPERM}) \\ &\quad [6.40] \quad \quad \quad [-1.16] \quad \quad \quad [+0.68] \\ &\quad + 0.0651 (\text{AFFIDX}) \\ &\quad \quad \quad [+0.70] \end{aligned}$$

Durbin-Watson = 188% R-Square = 65% Adj. R Square = 60% F Stat = 13.26

Seattle

$$\begin{aligned} \text{APT RETURN} &= 06.95 + 4.0687 (\text{EMP}) - 4.2262 (\text{POP2544}) - 0.0082 (\text{MFPERM}) \\ &\quad [5.97] \quad \quad \quad [-3.57] \quad \quad \quad [-0.28] \\ &\quad - 0.1185 (\text{AFFIDX}) \\ &\quad \quad \quad [+1.08] \end{aligned}$$

Durbin-Watson = 136% R-Square = 60% Adj. R Square = 54% F Stat = 10.75

Portland

$$\begin{aligned} \text{APT RETURN} &= 09.50 + 0.6728 (\text{EMP}) - 1.7105 (\text{POP2544}) + 0.0042 (\text{MFPERM}) \\ &\quad [0.47] \quad \quad \quad [-0.92] \quad \quad \quad [+0.13] \\ &\quad - 0.9658 (\text{AFFIDX}) \\ &\quad \quad \quad [-3.20] \end{aligned}$$

Durbin-Watson = 180% R-Square = 45% Adj. R Square = 36% F Stat = 04.89

Denver

$$\begin{aligned} \text{APT RETURN} &= -2.49 + 5.8722 (\text{EMP}) + 5.7800 (\text{POP2544}) - 0.0030 (\text{MFPERM}) \\ &\quad \quad \quad [6.24] \quad \quad \quad [+2.20] \quad \quad \quad [-0.76] \\ &+ 0.1321 (\text{AFFIDX}) \\ &\quad \quad \quad [+0.49] \end{aligned}$$

Durbin-Watson = 107% R-Square = 59% Adj. R Square = 54% F Stat = 11.56

Phoenix

$$\begin{aligned} \text{APT RETURN} &= -0.30 + 3.3780 (\text{EMP}) - 1.1144 (\text{POP2544}) + 0.0324 (\text{MFPERM}) \\ &\quad \quad \quad [4.30] \quad \quad \quad [-0.87] \quad \quad \quad [+2.36] \\ &+ 0.5221 (\text{AFFIDX}) \\ &\quad \quad \quad [+1.67] \end{aligned}$$

Durbin-Watson = 200% R-Square = 57% Adj. R Square = 51% F Stat = 09.73

Salt Lake City

$$\begin{aligned} \text{APT RETURN} &= -5.90 + 3.3520 (\text{EMP}) + 6.2111 (\text{POP2544}) + 0.0053 (\text{MFPERM}) \\ &\quad \quad \quad [1.54] \quad \quad \quad [+1.99] \quad \quad \quad [+0.34] \\ &+ 0.2984 (\text{AFFIDX}) \\ &\quad \quad \quad [+1.24] \end{aligned}$$

Durbin-Watson = 106% R-Square = 28% Adj. R Square = 15% F Stat = 02.12

Albuquerque

$$\begin{aligned} \text{APT RETURN} &= 3.99 - 0.5010 (\text{EMP}) - 10.1478 (\text{POP2544}) - 0.00019 (\text{MFPERM}) \\ &\quad \quad \quad [-0.31] \quad \quad \quad [-2.96] \quad \quad \quad [-0.24] \\ &- 0.0575 (\text{AFFIDX}) \\ &\quad \quad \quad [-0.52] \end{aligned}$$

Durbin-Watson = 199% R-Square = 85% Adj. R Square = 77% F Stat = 10.01

Las Vegas

$$\begin{aligned} \text{APT RETURN} &= 4.67 + 0.9460 (\text{EMP}) - 00.3167 (\text{POP2544}) + 0.04962 (\text{MFPERM}) \\ &\quad [+2.80] \qquad \qquad \qquad [-0.57] \qquad \qquad \qquad [+3.45] \\ &+ 0.0867 (\text{AFFIDX}) \\ &\quad [+0.50] \end{aligned}$$

Durbin-Watson = 216% R-Square = 58% Adj. R Square = 50% F Stat = 07.60

Tucson

$$\begin{aligned} \text{APT RETURN} &= 8.18 + 3.6110 (\text{EMP}) - 01.0002 (\text{POP2544}) - 0.00149 (\text{MFPERM}) \\ &\quad [+2.41] \qquad \qquad \qquad [-0.64] \qquad \qquad \qquad [-0.50] \\ &- 0.6396 (\text{AFFIDX}) \\ &\quad [-1.94] \end{aligned}$$

Durbin-Watson = 160% R-Square = 36% Adj. R Square = 27% F Stat = 03.99

Portfolio Optimization and Determination

Modern Portfolio Theory (MPT) (Markowitz method/Mean Variance Analysis)

Once the variables have been produced from the raw data, and the series have been tested for statistical significance, we can now input the information into the optimization model.

Software Determination

Prior to collecting the data, we conducted an extensive search to determine the appropriate software package for this analysis. Aside from custom programs and in-house programming, we identified three programs capable of running the optimization procedures. The first program by Ibbotson & Associates was capable of running the analysis but the cost of the program was prohibitive. The second program by MatLab was overly technical and could not run on our current computer platform. The third program, Excel Solver, was recently upgraded and released, and was provided to at a deep academic discount.

Model Determination

Before running the optimization model, we need to impose some constraints. These constraints consisted of minimum and maximum portfolio weights by metro area, target returns for the portfolio over the forecast period, and the level of risk the company would be willing to incur to achieve those target returns.

Metro weight ranges were determined based on: 1) the size of the market by units, 2) the depth and breath of the Class A investment market, 3) where the market is in its apartment and business cycle, and 4) future economic and apartment market fundamentals. Weight ranges were determined based on these criteria and reviewed by top management for reasonableness.

Expected returns used as inputs into the model were determined by taking the median or average return for the metro area over the sample time period. This could be viewed as a long-term structural growth rate for the metro area, assuming that metro areas move in and out of equilibrium but always revert back to some structural mean. Forecast returns were also calculated on an annual basis for the five-year period from 1998 to 2003. The assumption is the portfolio should be weighted based on predicted market performance.

Variances or standard deviations (risk) associated with given return levels were determined from the distributions of total returns and standard deviations. This method allowed us to determine the appropriate risk level associated with the given level of return. See Tables 1 – 3 below.

TABLE #1: MEAN TOTAL RETURN RANKINGS			
(1986-2000)			
Rank	State	Metro Area	Mean Total Return %
1	UT	Salt Lake City*	17.4%
2	CA	SF Bay Area*	15.9%
3	CA	Los Angeles	15.0%
4	CA	Sacramento	14.8%
5	NM	Tucson	14.6%
6	WA	Seattle	14.5%
7	AZ	Phoenix	14.5%
8	USA	USA	14.4%
9	CO	Denver	14.4%
10	CA	San Diego	13.9%
11	CA	Orange Co	13.7%
12	OR	Portland*	13.1%
13	CA	Riverside	12.4%
14	NV	Las Vegas*	11.4%
15	AZ	Albuquerque*	8.3%
Source: National Real Estate Index, Regional Financial Associates and BRE Properties			

* These Metros date back to:
Alb-1996, Las-1990, Pot-1989, Say-1990, Sfo-1990

Forecast Apartment Market Returns are calculated using a forecast model which utilizes a regression of independent variables (Employment, Population, Multi-Family Permits and Affordability Index) and Actual Apartment Market Returns.

TABLE #2: STANDARD DEVIATION TOTAL RETURN RANKINGS (1986-2000)

Rank	State	Metro Area	Std Dev Total Return %
1	AZ	Albuquerque*	3.4%
2	USA	USA	4.7%
3	CA	Sacramento	6.5%
4	NV	Las Vegas*	6.5%
5	CA	Orange Co	7.4%
6	OR	Portland*	8.2%
7	CA	SF Bay Area*	8.5%
8	WA	Seattle	9.0%
9	CA	San Diego	9.1%
10	CA	Los Angeles	9.8%
11	UT	Salt Lake City*	10.2%
12	CO	Denver	10.9%
13	AZ	Phoenix	11.1%
14	NM	Tucson	11.1%
15	CA	Riverside	11.7%

Source: National Real Estate Index, Regional Financial Associates and BRE Properties

TABLE #3: MEAN / STD DEV TOTAL RETURN RANKINGS (1986-2000)

Rank	State	Metro Area	Mean Total Return/ Std Dev
1	USA	USA	3.06
2	AZ	Albuquerque*	2.42
3	CA	Sacramento	2.26
4	CA	SF Bay Area*	1.88
5	CA	Orange Co	1.84
6	NV	Las Vegas*	1.75
7	UT	Salt Lake City*	1.70
8	WA	Seattle	1.62
9	OR	Portland*	1.59
10	CA	San Diego	1.53
11	CA	Los Angeles	1.53
12	CO	Denver	1.32
13	NM	Tucson	1.31
14	AZ	Phoenix	1.31
15	CA	Riverside	1.05

Source: National Real Estate Index, Regional Financial Associates and BRE Properties

Model Results

Base on the single index and multiple index regression approaches, and forecast and historical mean returns, optimal weight ranges were determined.

Due to the nature of the optimization model program, weights were maximized for higher return metro areas, and weights were minimized for lower return metro areas. Higher return metro areas tended to be smaller mountain state metro areas, and lower return metro areas tended to be larger Pacific Northwest and California metro areas.

Due to the extreme nature of the metro weight results more emphasis shall be placed on the multiple index model. This model takes into account more than one influence (supply and demand variables) on apartment returns for the metro area.

Weight Variances (actual)

Once the optimal weights have been calculated they can be compared to the actual weights of the apartment portfolio. The optimal weights minus the actual weights by metro area gives a weighted variance. This variance gives the degree of over or under concentration by percent for the portfolio. These weight variances can then be used, once multiplied by the target portfolio size, to help determine acquisition and disposition strategy going forward for the next three to five years.

These optimal vs. actual variances can be calculated by units, net asset value, total funds from operations, net operating revenues depending on performance measures determined by upper management.

Market Location Quotient

Market Location Quotient (MLQ) shows where the portfolio is over and under concentrated compared to the optimal portfolio. The MLQ is REIT's portfolio concentration by market divided by the optimal portfolio concentration by market. If the ratio is greater than one then the portfolio is over concentrated in that given market compared to the optimal portfolio, if the ratio is less than one then the portfolio is under concentrated in that given market.

Role of the Delphi Team in Setting Portfolio Strategy

The Delphi Team approach takes into consideration the qualitative aspects of portfolio diversification. The implementation or acquisition plan takes into consideration both the quantitative results of the geographic and economic base diversification and optimization model, and the qualitative aspects or knowledge of an expert panel for determining the final portfolio weights.

Acquisition and Development Portfolio Strategy

Active Portfolio Style

The active portfolio style is the Markowitz optimization model discussed earlier in the analysis. This approach is active in the sense that you can vary the risk and returns depending on portfolio return requirements or levels of risk tolerance.

Passive Portfolio Style

The passive portfolio approach is similar to the stock market index approach where you replicate the market. The assumption is that you can diversify away your unsystematic risk by going into different geographic areas, but you cannot diversify away your systematic risk. So it makes sense to just become the market and eliminate transaction costs. You can then use these transaction fees to enhance your overall portfolio returns.

Investment Acquisition/Disposition Time horizon

Implementation of the acquisition/disposition process to optimize the portfolio shall occur over a three to five year period. The portfolio optimization model shall be run and upgraded on a biannual basis. The goal is to reach the optimal portfolio allocations within a three to five year period. Within this period, certain segments of the portfolio shall be acquired and disposed of based on other portfolio strategies such as cycle timing and trading systems.

Acquisition and Disposition Strategy: An Iterative Process

The iterative process is a very simplistic approach to optimizing the portfolio. It starts by looking at our portfolio allocation and the optimal allocation by units, then takes the variance between the two. Dividing the variance in units by 250 units to get the number of projects we need to divest or invest in to get at the optimal allocation. If the assumption is that we do not sell then you would buy into the positive variance markets until the variance approaches close to one or two projects. It may take three iterations before the portfolio approaches the optimal weights.

The problem for the iterative allocation process is that it may take five years to optimize the portfolio, because buying and selling real estate is very lumpy, inefficient, takes time along with all the problems associated with real estate transactions.

Economic Base Diversification and Portfolio Optimization

The economic base diversification and portfolio optimization approach is phase II of the analysis.

This approach to portfolio diversification and optimization is conducted similar to the geographic approach in that we can use both the passive and active management strategy or style.

The passive approach is to index the portfolio according to the distribution of industry employment across the western region, and the active approach is to look at employment trends by industry across the western region.

The active approach using the Markowitz Model would substitute metro areas in the geographic model industries in the economic model. Industries would consist of 13 economic based categories that have already been developed for the Western Region by Regional Financial Associates. These industries would include technology, durable goods, high technology, government, gaming, hotels and resorts, etc.

The economic base model would allow us to use basically same structural model use for the geographic diversification model. We would be looking at industries within the western region instead of the metro areas, with the question being "How do you want to distribute or optimize the portfolio across industries?" Once you have determined the optimal allocation by industry category, we look how our portfolio is distributed by industry. From this analysis we can identify where we are over and under concentrated by industry, then identify what metro areas we would want to enter to balance out the portfolio's economic concentration.

Reconciling the Two Approaches to Portfolio Diversification and Optimization

Geographic and economic base diversification and optimization results should be reconciled. The geographics tell us how we want to be distributed geographically and the economics tells us how we want to distribute economically. For example, using the economic base diversification with a passive style, we are over concentrated in high tech, but we may be under-concentrated in durable goods manufacturing. To diversify the portfolio we would want to invest in a metro area with a high concentration of durable goods manufacturing, Denver and Seattle.

The goal of this strategy is to look towards markets understanding how they are over and under-concentrated by industry and how we want to allocate our assets. We are looking at the portfolio from both its geographic distribution and the characteristics of individual metro areas by industry. For example, right now BRE Properties portfolio is over concentrated in the Bay Area and in high-tech using the passive portfolio approach.

Portfolio Diversification and Optimization using a Cycle or Market Timing Approach

In addition to the geographic and economic base diversification and optimization approaches, certain components of the portfolio should be looked at from a more opportunistic view. The view is to enhance portfolio yields by trading assets in and out of the portfolio based on where the markets are within their property cycle. This approach is a portfolio yield enhancement strategy that take advantage of markets that have move into short-term disequilibrium conditions. The objective to exploit short-term overbought and oversold market conditions.

For example, Phoenix seems to be a market that has hit a soft spot in its cycle, in the long run it will be a good market, and currently we are over-concentrated in that market. We may want to sell into this market due to a good economy and the fact that investment capital is still flowing into the market. Since there is liquidity we may want to sell, take the proceeds and purchase property in Los Angeles which is in the early phases of its recovery and the construction cycle and is under weighted in our portfolio.

By paring back in Phoenix, closer to our optimal allocation, we can reallocate our resources into Los Angeles to take advantage of the long-term fundamentals and cure a severely under-weighted portfolio condition.

RESEARCH RESULTS II: PORTFOLIO DIVERSIFICATION AND OPTIMIZATION

The Geographic Diversification Model

The geographic diversification model produces results that indicate those Western metros which, based on both historical and projected supply and demand factors, are likely to produce the highest risk-adjusted rate of return over a five-year horizon.

Forecast Model Variables

The independent, or explanatory, variables used in this model are year-over-year changes in:

- Employment
- Population of persons age 25-44
- Housing affordability index, and
- Multifamily permits

The dependent, or predicted, variable is annualized total apartment returns from 1987-2003.

Optimization Model Constraints

- Management set subjective limits on the minimum and maximum N.O.I values the model could allocate to any individual metro.

	<u>MIN</u>	<u>MAX</u>
So. California	8%	17%
Sacramento	3%	8%
San Diego	3%	10%
Las Vegas	3%	8%
Phoenix	3%	12%
Tucson	3%	8%
Denver	3%	10%
Albuquerque	1%	5%
Portland	3%	8%
Salt Lake City	2%	8%
Seattle	3%	15%
Bay Area	10%	20%

- The model retains California exposure of at least 50%.
- The model is moderately constrained allowing adequate range for the optimization program to derive efficient allocation points.

Assumptions

- A passive national apartment portfolio could be expected to produce an average annual total return of approximately 12% (based on an average cap rate of 9% with 3% capital appreciation based on a long-term rate of inflation).
- The REIT's active, regionally focused model portfolio assumes a slightly higher level of both risk and reward, predicting an annual total return of 15%.

Optimal Weights and Projected Annual Total Returns

Using the variables, constraints and assumptions listed above, the geographic diversification model indicated the following optimal weights. The optimal weights were determined by total annual returns produced by the forecast model and subjective constraints imposed by management. The expected portfolio return maximizes yield for a given level of risk above the national average.

Metro Area	Optimal Weights	Predicted Total Annual Returns
Los Angeles/Orange Co./Riverside	15.0%	19.3%
San Diego	10.0%	16.0%
SF Bay Area	20.0%	15.5%
Seattle	15.0%	15.0%
Phoenix	12.0%	13.6%
Denver	10.0%	13.5%
Sacramento	6.0%	13.0%
Tucson	3.0%	12.5%
Portland	3.0%	11.0%
Salt Lake City	2.0%	10.0%
Las Vegas	3.0%	9.5%
Albuquerque	1.0%	8.5%
Total Portfolio	100%	14.9%

1) Predicted Total Annual Returns = expected income or cash flow returns plus capital appreciation.

The Market Selection Model

To support the findings of the geographic diversification model, the market selection model was re-run as a comparative tool. This model features a point scoring system for each metro using 13 variables versus the geographic optimization model's four variables.

Market Selection Model Supply and Demand Variables		Weights
Market Control Factors:		
Market Cycle Component 1998		5.0%
Economic Diversity Index 1997		10.0%
Risk-Adjusted Returns 1987 - 1997		3.0%
Employment Volatility 1987 - 1997		9.0%
Total Households 1998		3.0%
Market Control Factor Weight		30.0%
Apartment Demand Factors:		
Average Housing Affordability 1998 - 2003		6.0%
Wages and Salaries Growth 1998 - 2003		3.0%
Absolute Change in Employment 1998 - 2003		10.0%
Absolute Change in Population between the ages of 25 and 44 years old 1998 -2003		7.0%
Apartment Demand Factor Weight		26.0%
Apartment Supply Factors:		
Total Residential Permits Issued to Total Household Formations Ratio 1998 - 2003		20.0%
Total Multifamily Permits Issued from 1998 to 2003 divided by Total Multifamily Permits Issued 1981 - 2003		7.0%
Total Multifamily Permits Issued from 1998 to 2003 divided by Total Residential Permits Issued 1981 - 2003		7.0%
Total Residential Permits Issued 1998 - 2003 divided by Total Residential Permits 1981 - 2003		10.0%
Apartment Supply Factor Weight		44.0%

The Models Compared

The results of each model produce similar relative rankings.

Geographic Diversification & Optimization Model Results

Metro Area	Optimal Weights	Annual Returns
LA/Orange/Riv	15.0%	19.3%
San Diego	10.0%	16.0%
SF Bay Area	20.0%	15.5%
Seattle	15.0%	15.0%
Phoenix	12.0%	13.6%
Denver	10.0%	13.5%
Sacramento	6.0%	13.0%
Tucson	3.0%	12.5%
Portland	3.0%	11.0%
Salt Lake City	2.0%	10.0%
Las Vegas	3.0%	9.5%
Albuquerque	1.0%	8.5%
Total Portfolio	100%	14.9%

Market Selection Model Results

Rank	State	Metro Area
1	CA	LA/Orange Co./Inland Empire
2	CA	San Diego CA MSA
3	WA	Seattle-Bellevue-Everett WA PMSA
4	CA	San Francisco CA CMSA
5	AZ	Phoenix-Mesa AZ MSA
6	CO	Denver CO PMSA
7	CA	Sacramento CA PMSA
8	AZ	Tucson AZ MSA
9	UT	Salt Lake City-Ogden UT MSA
10	OR-WA	Portland-Vancouver OR-WA PMSA
11	NM	Albuquerque NM MSA
12	NV-AZ	Las Vegas NV-AZ MSA

Economic Base Diversification

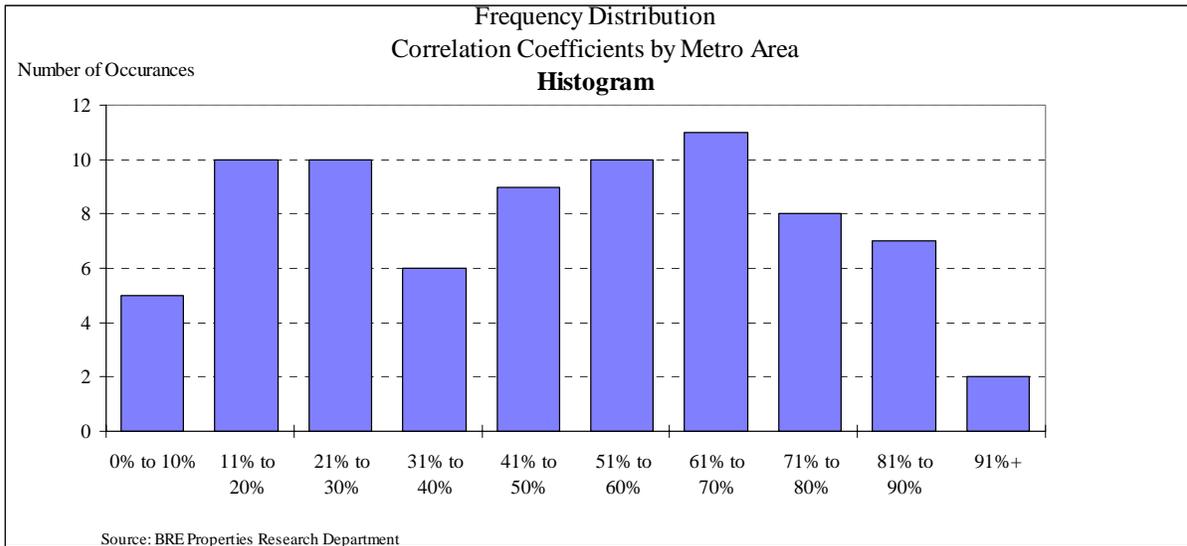
Metro Area Correlation Analysis

Employment growth is the most statistically significant variable for predicting apartment rent growth, total expected return and risk. The correlation coefficient between year-over-year percent change in total employment indicates moderately-high positive correlation between the Western and Mountain state metros. Of the 13 metro areas, there is a total of 78 possible correlation combinations, 51 correlation coefficients are below 60%, and 15 are below 20%.

Correlations lower than 60% indicate significant opportunities for reducing portfolio risk through diversification across geographic regions. Diversification benefits from a Western real estate portfolio diversification strategy is also reflected in the histogram's binomial distribution, indicating that there are opportunities for investment in metro areas with low correlations to other metro areas. Investments in high growth-low correlation markets eliminates over concentration both geographically and by industrial economic base.

CORRELATION COEFFICIENTS BY METRO AREA													
From Second Quarter 1976 to First Quarter 1996													
<i>Year-Over-Year Change in Total Employment Growth by Quarter</i>													
	<i>Omg.Co.</i>	<i>LA Area</i>	<i>San Diego</i>	<i>Riv.-S.B.</i>	<i>Den.</i>	<i>Phox.</i>	<i>Tuc.</i>	<i>Sl.Lk.Cit.</i>	<i>LasVeg.</i>	<i>Seac.</i>	<i>Portl.</i>	<i>Sac.</i>	<i>S.F.Bay</i>
Omg.Co.	100%												
LA Area	94%	100%											
San Diego	90%	91%	100%										
Riv.-S.B.	59%	66%	80%	100%									
Den.	19%	23%	10%	-7%	100%								
Phox.	53%	57%	50%	44%	47%	100%							
Tuc.	24%	22%	16%	9%	38%	75%	100%						
Sl.Lk.Cit.	7%	17%	13%	28%	67%	63%	41%	100%					
LasVeg.	16%	31%	28%	49%	34%	52%	26%	70%	100%				
Seac.	73%	75%	82%	83%	15%	39%	13%	21%	43%	100%			
Portl.	53%	56%	58%	68%	39%	62%	30%	67%	76%	74%	100%		
Sac.	66%	78%	84%	80%	4%	46%	12%	24%	48%	66%	54%	100%	
S.F.Bay	89%	88%	83%	51%	39%	50%	18%	19%	24%	69%	56%	68%	100%

Sources: Regional Financial Associates and BRE Properties Research Department.
 Correlation coefficient measures the degree to which employment trends between the two employment series move together over time. Correlation close to 1.0 indicates exact positive movements between the two series, and -1.0 indicates exact opposite movements.



Preliminary Economic Base Analysis

In the economic base analysis, the diversification inherent to the REIT's current portfolio¹ was measured against the economic diversification of the U.S. as a whole.

The economic diversification of the REIT's current portfolio is similar to that of the U.S. in the areas of:

- Transportation and distribution
- finance and insurance
- locally driven services
- retail trade, and
- federal, state and local government

The REIT's portfolio is under or over concentrated in the following industries. (The numbers to the right indicate the REIT's level of concentration relative to the U.S.)

High Over-Concentration		Moderate Over-Concentration	
High Tech	1.7x	Travel & Entertainment	1.4x
Aircraft/Defense	3.1x	Construction & Real Estate	1.2x
		Business & Professional Services	1.1x

High Under-Concentration		Moderate Under-Concentration	
Manufacturing, Non-Durable Goods	.4x	Manufacturing, Consumer Non-Durables	.8x
Manufacturing, Automobiles	.4x	Hospitals/Medical Labs	.7x
Private Universities	.4x	Manufacturing, Consumer Durables	.7x
		Energy Utilities & Mining	.7x

- 1) "Current" portfolio is defined as all stabilized portfolio assets plus all committed development properties as of September 1998.
- 2) Detailed economic and geographic concentration analysis and industrial class definitions are presented in the Appendix.

Mitigating Industry Concentrations

Significant industry over/under concentrations in the portfolio can be equalized by adjusting allocations to the following metros:

Significant Over Concentrations			
Industry		Defensive Markets	
High Tech	1.7x	Las Vegas	.4x
		Tucson	.9x
Aircraft/Defense	3.1x	Denver	.1x
		Las Vegas	.1x
		Portland	.6x

Significant Under Concentrations			
Industry		Defensive Markets	
Manufacturing (Non-durable intermediary products)	.4x	So. Cal	.8x
		Portland	.8x
		Salt Lake	.5x
Manufacturing (Automotive)	.4x	Salt Lake	1.6x
		Portland	.9x
		Phoenix	.7x
Private Universities	.4x	So. Cal	.9x
		Portland	.8x
		Bay Area	.8x

Note: Full defensive market industry concentrations are provided in Appendix #3-Tables 4-5 of this report

Integration of Results

Integrating the results of the geographic diversification and market selection models with the economic base analysis suggests the following three-five year investment allocation to double the current size of the REIT's portfolio.

RESEARCH RESULTS II: DELPHI PROCESS

Delphi Process

Definition of Delphi Process

The term Delphi was taken from ancient Greek mythology, where people turned to the gods for answers and questions to problems that worried them. The answers and shrine from which advice came was called the Oracle of Delphi. The Delphi Team and Modified Delphi Process was taken from a technique developed at the RAND Corporation in the mid-1960s. This method refines the opinions of experts in a particular field regarding future product, industry or economic conditions.

Statement of Purpose

The purpose of the Delphi Process and Delphi Team is to provide personal operating and market insights and judgments into the portfolio allocation decision making process.

Goals and Objectives

The goals and objectives of the Delphi process are to take advantage of expert knowledge imbedded in management and board of directors, and provide these experts with an opportunity to comment on portfolio conditions, helping to set portfolio allocation policy.

Activities

At the first meeting of the REIT's Delphi Committee, members reached consensus on two items: desirable attributes of a model portfolio and characteristics of "core" markets. The group then discussed positive and negative attributes of each of the REIT's markets.

Before deciding on metro area allocations, the Delphi Team took other qualitative factors into consideration before making their recommendations: portfolio attributes, core market characteristics, market summaries, and market exit considerations.

Preliminary discussion points on reasons to stay in non-core markets and tactical issues surrounding exit strategies in non-core markets are included in the Appendix.

RESEARCH RESULTS II: EXPECTED OUTCOMES BACK TESTING THE FORECAST MODEL

Description of Back Test Process and Findings

Test Results: 70% of the time the forecast model predicts actual apartment returns, effective rent growth and vacancy rate rankings since 1987.

General Test Results:

- **High Correlation Between** Actual and forecast total apartment return rankings by metro area over time; and Actual and forecast total apartment return rankings with that of effective rent growth rankings by metro area over time.
- **Moderate-High Correlation between** actual and forecast total apartment return rankings with vacancy rate rankings by metro area over time.

Back Test Objective:

- The purpose of the back test is to quantify the predictive capability of the total return model to signal major movements in metro area rankings over time.
- The primary objective of the back test is to measure how accurate the model is in predicting movements in metro area rankings by total return since 1987.
- The secondary objective of the back test is to confirm model accuracy through the use of real estate market variables that are out side that of the forecast model itself.

Back Test Methodology: Rank Correlation Analysis

- To compare forecast model performance against actual real estate market performance over time, **Rank Correlation Analysis (RCA)** was employed.
- RCA tests for co-movements in metro area rankings across time.
- RCA was employed to test for co-movements in *forecast apartment return rankings* with that of *actual apartment return rankings, actual effective rent growth rankings* and *actual vacancy rate rankings* over a rolling three-year period since 1987.

Actual Variables Tested:

One real estate capital market variable was use for *forecast model verification* and validity; and two real estate space market variables were used for *economic-theoretical verification* and validation.

- **Capital Market Variable**: Rolling actual three-year total apartment returns by metro area were generated from current income yields (cap rates) and capital appreciation (change in sales price per square foot) using National Real Estate Index (NREI) data.
- **Space Market Variable**: Two space market variables were used to see if movements in total forecast returns by metro area correspond with that of high effective rent growth and low vacancy rates over the three-year forecast period.
 - ***Effective Rent Growth***: Three-year average annual compound growth rates by metro area were calculated from effective rents using REIS, Inc. data.
 - ***Vacancy Rate***: Three-year average vacancy rates by metro area were calculated using REIS, Inc. data.

Variable Assumptions:

- Based on statistical inference, it is assumed that forecast apartment returns are highly correlated with actual apartment returns.
- Based on real estate economic theory, it is assumed that total apartment returns are highly correlated with effective rent growth due to it being a significant component of current NOI yields; and moderately correlated with vacancy rates due to lags in rent spikes as vacancy rates approach frictional levels.

Summary Graph and Table

Note: The Summary Graph and Table identifies the degree to which the forecast model predicted movements in rankings by metro area over time, given that the forecast rank fell within four ranks from the actual.

For Example:

The *Summary Graph* shows that 70% of the time, the Forecast Model predicted total return rankings which corresponded to actual apartment returns, effective rent growth and vacancy rate rankings—falling well within an error tolerance level of 0 – 4 ranks; and of this 70%, 65% fell within 0 – 2 ranks and 35% fell within 3 – 4 ranks.

The *Summary Table* shows that the model predicted actual apartment return rankings roughly 100% of the time for Denver, Las Vegas and Seattle; effective rent growth rankings roughly 100% - 90% of the time for Las Vegas, Denver and the Bay Area; and vacancy rate rankings roughly 90% - 80% of the time for Seattle, Las Vegas and Sacramento.

See Appendix for individual metro area Back Test analysis and results.

RESEARCH RESULTS II: PERFORMANCE EVALUATION BENCHMARKING THE PORTFOLIO

Introduction

The purpose of this benchmarking process is to help understand where the portfolio is relative to actual market and research projections. The report measures the performance of the overall portfolio relative to the benchmark, and helps identify differences between actual portfolio performance by market, and data reported by a third-party research firm, and projections by internal research. This section of the report identifies sources of data, relevant comparisons and analysis.

Methodology

External Data

There are three providers of apartment market data that cover all or the majority of the REIT's markets: REIS Reports, RealFacts and MP/F Research. REIS covers ten of the major markets. REIS Reports does not cover: Salt Lake City, Las Vegas, Tucson and Albuquerque, and updates only certain markets at certain times throughout the year. RealFacts will be reporting on all of markets by the end of 1999. It will be another year before RealFacts can provide year-over-year data in second tier markets: Las Vegas, Tucson, and Albuquerque.

MP/F Research is the only data provider that is currently reporting physical occupancies and asking rent growth in all of markets on a quarterly basis. Quarterly statistics are released eight to 10 weeks after the end of the quarter. Another caveat to MP/F data is in markets where there is a spike in new construction, or high levels of new construction.

In the short-term, asking rents can be skewed upward as new higher-cost product enters the market. This upward bias can make rent growth in under performing markets look better than it actually is. In the long-term, as the market absorbs new supply, asking rent growth will reflect the underlying supply and demand fundamentals of the market. For example, during the second quarter of 1998, as reported by MP/F, year-over-year asking rent growth for Portland spiked 9.4% as new supply entered the market, but as excess supply conditions continued, asking rent growth declined to less than 1.5% year-over-year through the second quarter of 1999.

MP/F data are collected and provided on a quarterly basis. The data are collected from professionally managed apartment communities. These respondents tend to be more aggressive during market upturns when reporting physical occupancies and rent growth, and tend to be less inclined to report falling occupancies and rent growth during market downturns. Data are collected either through questionnaires completed by apartment community owners or managers or directly from internal management reports.

In the current survey, statistically significant sample sizes are used to calculate physical occupancy and asking rents for the quarter. Sample sizes for our markets are:

MP/F Research Metro Area Sample Sizes	
Metro Area	Sample Size (Units)
Albuquerque	6,500
Denver	20,600
Las Vegas	18,200
Los Angeles	12,130
Orange County	10,200
Phoenix	51,500
Portland	12,250
Riverside	8,245
Sacramento	6,200
Salt Lake City	6,500
San Diego	10,700
San Francisco Bay Area	17,700
Seattle	18,335
Tucson	9,645

Physical occupancy rates are as of quarter end and asking rent growth is a year-over-year percent change as of quarter end.

MP/F provides quarterly occupancy and rent growth statistics two months after the quarter end, on disk and in report format.

Internal REIT Data

REIT Asset Management Data

The REIT's Asset Management group produces physical occupancy rate statistics on a weekly basis. For benchmarking purposes, the same-store physical occupancy for the portfolio, and for each market, will be as of the last week of the quarter. Same-store asking rent growth is calculated on a calendar, year-over-year basis as of the last week of the quarter.

The methodology for calculating same-store rent growth takes gross potential rent from the general ledger, representing leased units at scheduled rents, plus vacancies at market, divided by the total number of units at the property. There is no break-out between unit mix. This represents the overall rent per unit for the community. Average rents are then aggregated up into unit weighted average same-store rents for the metro area. Year-over-year rent change is then calculated for each market.

The benefit of using this methodology is its consistency with reported same-store financials. The caveat to this approach is it is backward looking and reflects actual economic rents for the portfolios over a specific period of time. This methodology is not necessarily consistent with the methodology used by MP/F Research, but does reflect the overall direction and pattern of rent growth, with a time lag.

Internal Research Department Data

The REIT's Research Department produces annual physical occupancy rate and effective rent growth statistics for the current year. Effective rent growth reflects projected asking rent growth less anticipated concessions. These projections are updated on a quarterly basis.

To make research comparable to the portfolio and MP/F, asking rent growth is produced from effective rent growth projections by adding back a Rent Concession Factor. This factor reflects the amount of concessions being made in the market, and its effect on asking rent growth. These concession factors can range from 50 to 200 basis points depending on projected market conditions.

For this analysis, two research statistics will be reported: static and updated. Static occupancy rates and asking rent growth will be current year projections as of the prior fourth quarter, and updated occupancy rates and asking rent growth will be the current year projections updated as of the most recent quarter end. This process allows for comparisons between the Research Department's original and updated occupancy rate and asking rent growth calculations with that of Asset Management and MP/F Research.

1999 Rent Growth Projection as of the Fourth Quarter 1998	BRE Rent Growth Projections		Rent Concession Factor
	Asking Rent Growth	Effective Rent Growth	
Albuquerque	-3.5%	-3.5%	0.0%
Denver	5.0%	4.5%	0.5%
Las Vegas	-2.5%	-2.5%	0.0%
Los Angeles	6.0%	5.0%	1.0%
Orange County	7.0%	6.0%	1.0%
Phoenix	3.0%	2.5%	0.5%
Portland	-2.0%	-1.5%	0.5%
Riverside-San Bernardino	3.5%	2.5%	1.0%
Sacramento	5.0%	4.5%	0.5%
Salt Lake City	4.5%	3.5%	1.0%
San Diego	6.5%	5.5%	1.0%
San Francisco Bay Area	6.0%	5.0%	1.0%
Seattle	5.5%	4.5%	1.0%
Tucson	4.0%	3.0%	1.0%

Analysis

The benchmarking analysis gives occupancy rate and asking rent growth statistics for the quarter for all 14 Western markets. Variances are calculated between REIT Actuals, Research static and updated, and MP/F Benchmark statistics. Overall performance of the portfolio is measured in three ways:

Benchmark Performance Ratios:

Note: Values greater than 100% indicate that the portfolio is outperforming the benchmarks, values less than 100% indicate that the portfolio is under performing the benchmarks.

Rent Growth Performance Ratio is portfolio same-store rent growth divided by MP/F's asking rent growth.

- For example, the REIT portfolio is currently 58.3% of the benchmark. This indicates that the portfolio is under performing the benchmark in regards to rent growth.

Occupancy Performance Ratio is actual occupancy rate divided by MP/F's occupancy rate.

- For example, the portfolio is currently 99.3% of the benchmark. This indicates that the portfolio is roughly on par with the benchmark in regards to occupancy rates.

Positive Variance Measurement:

Positive Variance Measure is the percent of positive variances divided by total variances.

Positive Variance Measure is the percent of positive variances divided by total variances.

- For example, there are currently 12 positive variances out of a total of 28, or 42.9%. The closer the percentage is to 100.0%, the greater the degree the portfolio is outperforming the benchmark, and the closer the percentage is to 0.0%, the greater the degree the portfolio is under performing the benchmark.

Results

Fourth Quarter 1999

- **Occupancy Performance Ratio dropped** slightly from 100.4% in the third quarter to **99.3%** in the fourth quarter of 1999.
- **Rent growth Performance Ratio improved** from 56.4% in the third quarter to **58.3%** in the fourth quarter of 1999.
- **Positive Variance Measurement Ratio dropped** from 46.4% in the third quarter to **42.9%** in the fourth quarter of 1999.

RESEARCH RESULTS II: PORTFOLIO EVALUATION ASSET SALES – EXIT STRATEGY – HOLD/SELL ANALYSIS

Introduction

After determining optimal portfolio weights, negative variances, and which markets and assets will under perform the benchmarks over the investment horizon, sale of assets and redeployment of capital is required for maximum return under active real estate portfolio management style. The decision to sell an asset is similar to supplemental appraisals or is more accurately viewed as equivalent to an acquisition underwriting.

The purpose is to evaluate the asset based on future financial performance. Renovation may be an option if Net Present Values (NPVs) are positive and Internal Rates of Return (IRRs) exceed hurdle rates. The decision to hold an asset is determined by total historical holding period yield and projected 10 year IRRs in excess of the company's target Weighted Average Cost of Capital (WACC). Effective exit strategies require the discipline to conduct comprehensive Hold/Sell Analysis (HSA) across the portfolio on an annual basis.

Procedures and metrics used in HSA:

- a. Evaluation of physical structure of building
- b. Capital Improvements
- c. Estimate of physical (economic) life
 1. Degree of physical and functional obsolescence
- d. Operating Analysis (Variance): Turnover
- e. Market Overview (Supply/Demand)
- f. Economic Analysis (Major Employer/Commercial Construction)
- g. Valuation (Hold/Sell) Analysis: Base Case, Worst Case and Best Case Rent Growth
 1. Actual vs. Market IRRs
 2. Actual vs. Market Cap Rates
 3. Actual vs. Market NPVs
 4. Market Price
 5. Replacement Costs
- h. Risks (Market/Property)
- i. Recommendation to Investment Committee
- j. Input/Goals/Asset Allocation/Capital Redeployment/Tax Strategy based on:
 1. Presence in Market
 2. Economies of Scale in Market
 3. Portfolio Diversification and Concentration
 4. Opportunistic selling

Metrics Used in Hold/Sell Decision Making

- a. Net Asset Value per Unit (Asset Management/Acquisition/Development)
- b. Comparable Sales Price Per Unit (Acquisition/Development)
- c. Total Replacement Cost Per Unit (Acquisition/Development)
- d. Rolling IRR Analysis (Asset Management/Research)

Rules Used in Hold/Sell Decision Making

- a. Set benchmark IRR (12%), calculate rolling 10 year NOI IRRs, as IRR peaks, starts to turn down, and approach IRR benchmark, make decision to sell or redevelop.
- b. Spread or ratio between sales price per square foot/unit and replacement cost per square foot/unit.
 1. For example, if the spread is significantly wide, sales price per square foot is 50% higher than replacement cost, the decision is to sell and invest in development projects.
- c. Spread or ratio between net asset value per square foot/unit and replacement cost per square foot/unit.
 1. For example, if the spread is significantly wide, NAV per square foot is 50% higher than replacement cost, the decision is to sell and invest in development projects.
- d. Spread or ratio between sales price per square foot/unit and net asset value per square foot/unit.
 1. For example, if the spread is significantly wide, sales price per square foot is 50% higher than net asset value, the decision is to sell and invest in other opportunistic markets because the market is overvaluing existing assets in the open market compared to its intrinsic value.

Supplemental Hold/Sell Analysis

- a. Sales and lease comparable analysis.
- b. Pipeline analysis (determine supply spikes and their impact on future occupancy rates and rent growth for the property).
- c. Overall market conditions (Phase of Cycle)
 1. Recommendations on when to enter/exit market.
 2. Recommendations on where to redeploy capital
 3. What is the strike price at which the property should be sold (target IRR).

EXAMPLE: HOLD/SELL ANALYSIS

July 2000

Fat Landing

Recommendation: **Decision**

DISCUSSION:

We recommendation holding the asset after extensive review of the market, asset condition, changing financial ratios, and the acquisition/disposition market liquidity.

IRR:	19%	Return On Book:	11.8%
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PROPERTY CHARACTERISTICS:

Region:	SFO	Submarket:	Foster City	Net SF:	414,918
Year Built:	1987	Year Rehab:	1996	Year Acq:	1996
Street Address:	000 Boot Drive Foster City, CA 94404			Total Units:	490

DESCRIPTION PROPERTY CONDITION:

The property has an extensive competitive advantage due to recent capital improvements, return on capital improvements. We may want to reposition the property to achieve higher yields and market rents. Minor issues associated with property condition and capital improvements.

3-Year Capital Improvements Schedule:

Item	Year	Cost
Roof – Rep. Flashing around chimneys	1-2-3	\$ 455,000
Building – storm drain, fitness center, tree removal, landscape		
Upgrade, repair tennis court wind screen	1-2-3	\$ 105,000
Equipment – pool/spa heaters	2001	\$ 12,000
Purchase – Rehab – cabinet and countertops	2-3	\$1,650,000
		\$
Total		\$2,222,000

OPERATING STATISTICS:

	1998	1999	2000 Budget
Economic Occupancy:	97.3%	95.8%	97.6%

Total Inc Growth:	10.1%	2.8%	6.8%
Operating Expenses Growth:	-1.5%	-1.8%	6.8%
Same Store NOI Growth:	14.1%	4.2%	6.8%

FINANCIAL STATISTICS:

Book Basis 12/99	\$64,015,00		
Original Investment	\$59,588,000		
Ownership Status	BRE (x)	DownREIT ()	Check One
Debt	\$	Debt Maturity	
Return on Book	11.8%		

MARKET CHARACTERISTICS

MARKET STATISTICS

BRE Research:

Metro Occ:	98.7%	Metro Eff Rent Growth:	23%	Cycle Phase:	2
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Sub-market Characteristics:

Sub-Mkt Occ:	97%	Sub Mkt Eff Rent Gr:	25%	Concessions:	N/A
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Overall market conditions are good: increasing traffic, rising rent pressures, falling notices, stronger renter demographics, lack of competition with apartments or housing, rising demand for property unit mix: sizes, types, quality, amenities, etc.

New Development within Last 12 Months:

Asset Name	Developer	Distance in Miles	Number of Units	Lease Start Date
Marlin Cove	M.H. Podel	.4 Miles	264	9/2000
Port O' Call	Pegasus	1 Mile	159	2001
Bay Meadows	JPI	2 Miles	575	2002

Employment Conditions:

High-tech employers expanding in area, financial services sector contracting in metro area and sub market. This will have a negative impact on the property now and in the next six months.

RESEARCH DESIGN III:

TIME DIVERSIFICATION PORTFOLIO STRATEGIES

An Introduction to Apartment Cycles

For decades the Western economy and apartment market has moved in and out of cycles, cycles of over and under supply. The source, amplitude and duration, of these cycles have varied over time. In the West we have seen many different types of cycles, cycles emanating from excessive land speculation, hyper inflation, depressions, recessions, banking crises, wars, etc. But one fact remains, markets, and cycles associated with them, are self correcting and have become less volatile over the years.

There are two fundamental sources that cause apartment market cycles to occur. These are employment demand-shocks and employment supply-shocks. Metro area apartment markets experiencing employment demand-shocks see high levels of job growth, high housing demand due to in-migration, positive net absorption, dropping vacancy rates below their long-run average, rising effective rents and sale prices above replacement costs, and eventually new construction (Bay Area, Orange County, Los Angeles, Seattle, San Diego).

Flows of new construction continue up to the point where the market moves back into balance, where sales prices drop below or are equal to the cost of construction. Depending on capital market conditions and metro area characteristics, the apartment market runs the risk of becoming oversupplied in the short-run, but in the long-run the market gravitates toward more balanced conditions.

Metro area apartment markets experiencing employment supply-shocks see low or falling job growth, low levels of housing demand due to out-migration, negative net absorption, rising vacancy rates above their long-run average, falling effective rents and sale prices below replacement costs, and eventually low or no new construction until the market reaches more balanced conditions (Albuquerque, Las Vegas, Tucson).

In both cases, the apartment market eventually self corrects and moves toward a state of balance, and remains in balance until the next employment shock. On average, a market in balance is said to be the point at which vacancy rates stabilize at roughly 5% and effective rents grow at the local inflation rate. This rule of thumb may vary slightly depending on the market.

Over the past 19 years, Western region apartment markets have gone through many different types of cycles. Some markets experiencing severe conditions of over and under supply (Albuquerque, Las Vegas, Phoenix and Tucson), some markets experiencing states of balance for long periods of time (Los Angeles, Bay Area, Seattle and San Diego), and some markets experiencing more modest conditions of over and under supply (Denver, Salt Lake City and Sacramento).

This article looks at historical apartment market cycles and current and future market conditions in the West, focusing mainly on the top 14 metro areas in regards to population. Metro areas analyzed are: Albuquerque, Denver, Las Vegas, Los Angeles, Orange County, Phoenix, Portland, Riverside, Sacramento, Salt Lake City, San Diego, Seattle, San Francisco Bay Area, and Tucson.

Apartment Market Characteristics

Metro areas in the West can be put into two groupings, supply-constrained or supply-unconstrained. This grouping allows us to understand and assess the trade-off between risk and return for these markets over the long-run.

Supply-constrained markets tend to be more: 1) urban, 2) have high barriers to development, 3) lack developable land, 4) have complex or difficult entitlement processes and 5) strict environmental regulations. Supply-unconstrained markets tend to be more: 1) suburban, 2) have low barriers to development, 3) have an abundance of developable land, and 4) have easy entitlement processes and 5) lack environmental regulations. Table #1 in the Appendix identifies those markets with supply-constrained and supply-unconstrained characteristics, along with other unique characteristics for the individual markets.

Total Return Comparisons

Supply-constrained markets are less likely to become oversupplied in the short-term, are less volatile, and provide higher real rates of return over the long-run. Supply-unconstrained markets are more likely to become oversupplied in the short-term, are more volatile, and provide high real returns in the short-run but lower real rates of return in the long-run.

Metro areas exhibiting the highest real rates of return over time are: the Bay Area, Salt Lake City, Seattle and Los Angeles; and metro areas exhibiting the lowest rates of return over time are: Las Vegas, Albuquerque, Riverside and Sacramento. As indicated in Table #2, supply-constrained markets tend to have higher rates of return over the long-run.

Table #2

Long-Run Total Apartment Returns			
Metro	Rank	Average Return *	Market Type
San Francisco Bay	1	14.7%	Constrained
Salt Lake City	2	14.4%	Constrained
Denver	3	13.7%	Un-Constrained
Seattle	4	13.1%	Constrained
Los Angeles	5	12.9%	Constrained
Phoenix	6	12.7%	Un-Constrained
Tucson	7	12.7%	Un-Constrained
San Diego	8	12.4%	Constrained
Sacramento	9	12.0%	Un-Constrained
Orange County	10	11.5%	Constrained
Riverside	11	10.9%	Un-Constrained
Portland	12	10.8%	Constrained
Albuquerque	13	9.0%	Un-Constrained
Las Vegas	14	8.0%	Un-Constrained

Source: Real rates of return were calculated by BRE Properties Research Department using data provided by the National Real Estate Index.

*Average annualized returns were calculated on a quarterly basis for years 1986-1998, except (Albuquerque 1996-1998), (Las Vegas, Salt Lake City, San Francisco 1990-1998), (Portland 1989-1998).

Note: Total real rates return were calculated using the year over year change in price per square foot plus the annualized income returns represented by the current cap rate, minus an average inflation rate of 3.0% per year.

Risk Comparisons

Supply-constrained markets tend to be less volatile or less risky than unconstrained markets in the long-run. Cycle risk is measured by the spread between the metro area’s highest and lowest vacancy rate. Supply-constrained markets tend to experience less volatility in vacancy rates and are less likely to experience extreme over and under supplied conditions.

Markets exhibiting the tightest spreads or least amount of cycle risk are: Orange County, Seattle, the Bay Area, and Los Angeles; and markets exhibiting the widest spreads or greatest amount of cycle risk are: Denver, Tucson, Phoenix and Albuquerque. Of all of the markets analyzed, Salt Lake City experienced the widest spread at 13%, due to the preference for and abundance of single-family housing construction.

Over the years, vacancy rate spreads have narrowed in the majority of supply-unconstrained markets. This is attributed to higher levels of bank regulation and the larger role of public

markets in allocating development capital. Tables #3 shows high-low vacancy rate spreads for supply constrained and unconstrained markets.

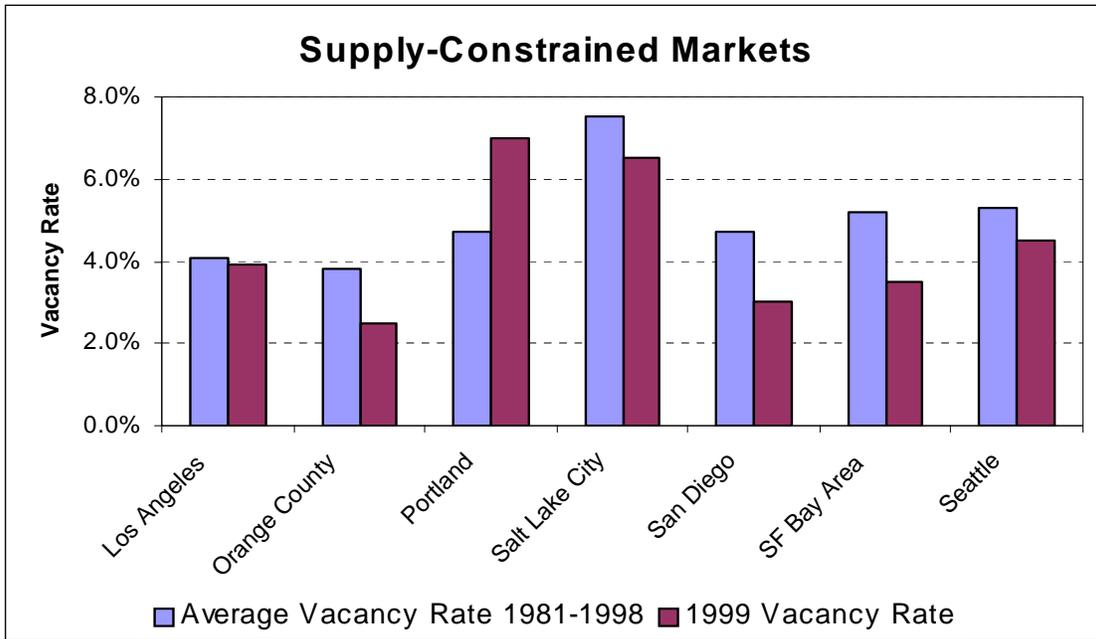
MAGNITUDE OF APARTMENT CYCLES IN THE WEST			
MEASURED BY VACANCY RATES SPREADS			
Metro Area	1981 - 1998 High	1981 - 1998 Low	1981 - 1998 High-Low Spread
Supply Constrained Markets			
Orange County	5.5%	2.0%	3.5%
Seattle	7.0%	3.0%	4.0%
Los Angeles	6.5%	2.0%	4.5%
San Francisco Bay Area	7.0%	2.5%	4.5%
San Diego	7.5%	2.0%	5.5%
Portland	8.5%	2.0%	6.5%
Salt Lake City	16.0%	3.0%	13.0%
Average for Supply-Constrained	8.3%	2.4%	5.9%
Supply-Unconstrained Markets			
Denver	13.9%	2.8%	11.1%
Tucson	15.0%	4.0%	11.0%
Phoenix	15.7%	5.5%	10.2%
Albuquerque	11.7%	3.2%	8.5%
Las Vegas	8.5%	2.7%	5.8%
Riverside	10.0%	5.5%	4.5%
Sacramento	7.0%	2.5%	4.5%
Average for Supply-Unconstrained	11.7%	3.7%	7.9%
Sources: MP/F Research, RealFacts, RealSource, REIS Reports, Marcus & Millichap, Clayton-Fillmore, ULI, and BRE Properties Research Department.			

Vacancy Rate Comparisons

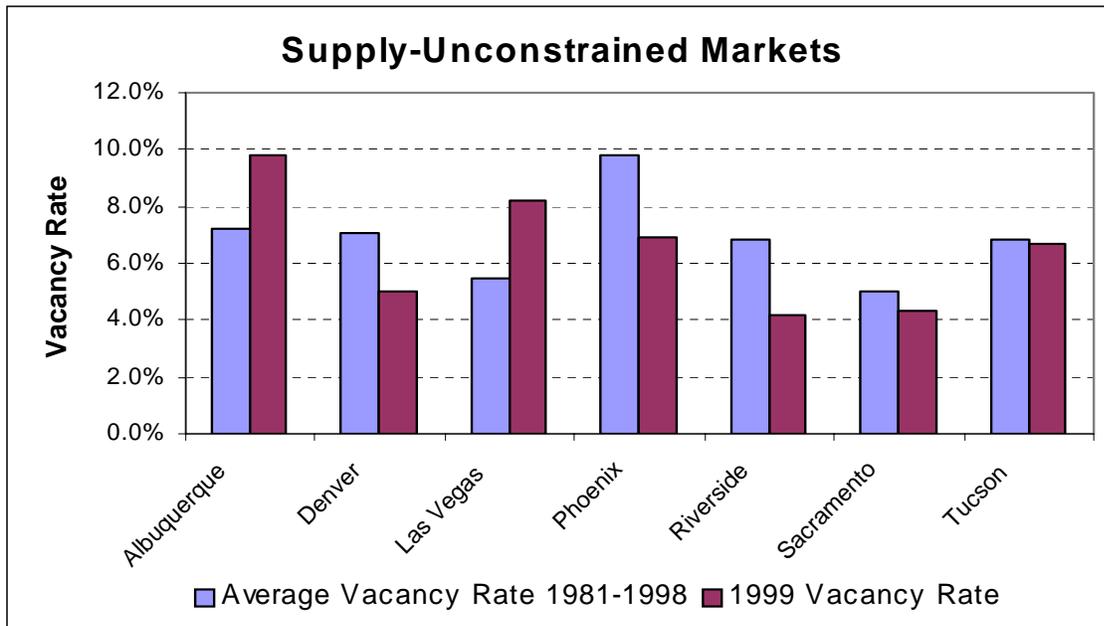
Current vacancy rates are also significantly lower than their long-term average for supply-constrained markets compared to supply-unconstrained markets. Current vacancy rates lower than long-term averages would indicate that the majority of Western apartment markets should experience above inflation rent growth, and that supply-constrained markets are expected to experience rent growth at levels well above the local inflation rate.

Supply-constrained markets with vacancy rates well below their long-term average are: Orange County, San Diego, the Bay Area and Seattle; and supply-unconstrained markets with vacancy rates below their long-term average are: Phoenix, Denver, Riverside and Sacramento. Graphs #1 and #2 compare long-term average vacancy rates to current vacancy rates for supply-constrained and unconstrained markets.

Graph #1



Graph #2



Effective Rent Comparisons

Supply-constrained markets are projected to have higher effective rent growth and lower vacancy rates than supply-unconstrained markets over the next three years. Markets expected to experience high effective rent growth are: Los Angeles, Orange County, San Diego and the Bay Area; while markets expected to experience low effective rent growth are: Albuquerque, Las Vegas, Portland and Phoenix. Table #4 shows metro area effective rent growth projections for supply-constrained and unconstrained markets.

Table #4

Effective Rent Growth Rankings				
Rank	Metro	Effective Rent Growth 1999-2001	Average Vacancy Rate 1999-2001	Market Type*
1	Los Angeles	6.0%	3.6%	SC
2	Orange County	5.7%	2.8%	SC
3	San Diego	5.2%	3.4%	SC
4	San Francisco Bay	4.3%	4.3%	SC
5	Denver	4.2%	5.2%	SU
6	Sacramento	4.0%	4.8%	SU
7	Riverside	3.8%	4.3%	SU
8	Seattle	3.8%	5.5%	SC
9	Tucson	2.7%	6.6%	SU
10	Salt Lake City	2.5%	6.0%	SC
11	Phoenix	2.3%	7.0%	SU
12	Portland	-0.5%	6.5%	SC
13	Las Vegas	-0.8%	7.4%	SU
14	Albuquerque	-2.2%	9.3%	SU

* Market Types: SC - Supply Constrained Markets, SU - Supply-Unconstrained Markets.
 Source: MP/F Research, RealFacts, RealSource, REIS Reports, Marcus & Millichap, Clayton-Fillmore, ULI, and BRE Properties Research Department.

Cycle Comparisons

Supply-constrained markets experience longer periods of time between cycles, limiting the risk of becoming oversupplied, thus adding to their return stability. Apartment vacancy rate cycles are measured by their peaks (high vacancy rates) and troughs (low vacancy rates) over time.

Supply constrained market cycles last roughly:

- 12 years from peak-to-peak, compared to 11 years for supply-unconstrained markets.
- 13 years from trough-to-trough, compared to 11 years for supply-unconstrained markets.
- 7 years from peak-to-trough, compared to 4 years for supply-unconstrained markets.

It takes longer for supply-constrained market cycles to go from high vacancy to low vacancy compared to unconstrained markets, thus mitigating the odds of experiencing boom-bust, and periods of rapidly rising and falling effective rents.

Metro areas exhibiting long time periods between cycles are: Los Angeles, San Diego, the Bay Area and Orange County; and metro areas exhibiting short time periods between cycles are: Las Vegas, Tucson and Riverside. Table #5 shows average time periods between cycles for supply-constrained and supply-unconstrained markets.

Table #5**APARTMENT VACANCY RATE CYCLES IN THE WEST BY TIME PERIOD**

Metro Area	Peak-to-Peak	Peak-to-Trough	Trough-to-Trough	Trough-to-Peak
Supply Constrained Markets				
Los Angeles	1993 to 2008 15 years	1993 to 2000 7 years	2000 to 2017 17 years	2000 to 2008 8 years
Orange County	1992 to 2004 12 years	2004 to 2010 6 years	1998 to 2013 15 years	1998 to 2004 6 years
Portland	1991 to 2000 9 years	2000 to 2004 4 years	1995 to 2004 9 years	1995 to 2000 5 years
Salt Lake City	1988 to 2000 12 years	2000 to 2007 7 years	1995 to 2007 12 years	1995 to 2000 5 years
San Diego	1987 to 2002 15 years	2002 to 2013 11 years	1988 to 2013 15 years	1998 to 2002 4 years
San Francisco Bay Area	1988 to 2003 15 years	2003 to 2010 7 years	1996 to 2010 14 years	1996 to 2003 7 years
Seattle	1993 to 2001 8 years	2001 to 2005 4 years	1997 to 2005 8 years	1997 to 2001 4 years
Average Duration in Years - SC	1990 to 2002 12 years	2001 to 2008 7 years	1995 - 2008 13 years	1995 - 2002 7 years
Supply-Unconstrained Markets				
Albuquerque	1988 to 1999 11 years	1999 to 2005 6 years	1994 to 2005 11 years	1994 to 1999 5 years
Denver	1986 to 2000 14 years	2000 to 2008 8 years	1994 to 2008 14 years	1994 to 2000 6 years
Las Vegas	1991 to 1999 8 years	1999 to 2003 4 years	1994 to 2003 9 years	1994 to 1999 5 years
Phoenix	1986 to 2000 14 years	2000 to 2008 8 years	1994 to 2008 14 years	1994 to 2000 6 years
Riverside	1997 to 2007 10 years	1997 to 2002 5 years	1993 to 2002 9 years	2002 to 2008 6 years
Sacramento	1989 to 2001 12 Years	2001 to 2008 7 years	1995 to 2008 13 years	1995 to 2001 6 years
Tucson	1997 to 2007 10 years	1997 to 2004 7 years	1994 to 2004 10 years	2004 to 2009 5 years
Average Duration in Years - SU	1990 to 2001 11 years	2001 to 2005 4 years	1994 to 2005 11 years	1994 to 2001 7 years

Notes: A **Peak** in the vacancy rate cycle is a peak in the vacancy rate and a **Trough** in the vacancy rate is the bottom of the vacancy rate cycle.

Sources: MP/F Research, RealFacts, RealSource, REIS Reports, Marcus & Millichap, Clayton-Fillmore, ULI, and BRE Properties.

Methodology

This analysis utilized multivariate statistics, Multivariate Analysis of Variance (MANOVA), the statistical procedure that involves more than one dependent variable (structural effective rent growth and occupancy rates).

MANOVA was selected to test the significance of group differences, the difference between structural effective rent growth and occupancy rates for supply constrained and unconstrained apartment markets in the western United States. MANOVA test whether mean differences among the two groups on a combination of the two dependent variables are likely to have occurred by chance.

Under the MANOVA approach, a new dependent variable is created, it is a linear combination of the original measured dependent variables, combined in a way that maximizes the group differences, it separates the two groups as much as possible. The new dependent variable is created by developing a linear equation where each measured dependent variable has an associated weight, and when combined and summed, creates maximum separation of group means with respect to the new dependent variable.

For this study, we are investigating the differences between constrained and unconstrained apartment markets in the western region, measured by structural effective rent growth and occupancy rates, for markets in different geographic areas. In this analysis, a new dependent variable is created, a linear combination of rents and occupancies. The new dependent variable would then be subjected to a univariate ANOVA by comparing variances on the new dependent variable for the two groups defined by geographic region.

Assumptions and Limitations

Multivariate analysis of variance assumptions:

- Observations must be randomly sampled and independent.
- Dependent variables must follow a multivariate normal distribution in each group.
- Population covariance matrices for dependent variables in each group are equal.
- Relationships among dependent variable pairs for each cell in data matrix are linear.

Statement of Research Question

Research Question: Do structural effective rent growth and occupancy rates differ by constrained (C) and unconstrained (U) markets?

Null Hypothesis: **H₀1:** Structural effective rent growth and occupancy rates will not differ by constrained and unconstrained markets.

Description of Population and Sample Data

- Apartment submarkets are made up of pre-defined geographic boundaries, defined by REIS Reports, Inc., New Jersey, and surveys are conducted on properties of 50+ units.
- 200 apartment submarkets in the western region:
 - San Francisco Bay Area
 - Sacramento
 - Seattle
 - Portland
 - Los Angeles
 - Orange County
 - San Diego
 - Phoenix
 - Denver
 - Salt Lake City
- Structural effective rent growth and occupancy rates for each submarket are average effective rent growth rates and occupancy rates from 1991 to 2000.
- See above text for definitions of supply constrained and unconstrained markets.

ANOVA Analysis and Results

Descriptive Statistics I

Positive and negative skewness for structural effective rent growth (EFFRNTSTRU) and occupancy rates (OCCRTSTRUC) require transformations. Square root transformations were used to mitigate positive and negative skewness in the data distribution.

Descriptives

			Statistic	Std. Error
EFFRNTSTRU	Mean		4.360E-02	1.487E-03
	95% Confidence Interval for Mean	Lower Bound	4.067E-02	
		Upper Bound	4.653E-02	
	5% Trimmed Mean		4.256E-02	
	Median		4.000E-02	
	Variance		4.423E-04	
	Std. Deviation		2.103E-02	
	Minimum		.00	
	Maximum		.10	
	Range		.10	
	Interquartile Range		3.000E-02	
	Skewness		.760	.172
	Kurtosis		-.113	.342
	OCCRTSTRUC	Mean		.9563
95% Confidence Interval for Mean		Lower Bound	.9542	
		Upper Bound	.9584	
5% Trimmed Mean			.9568	
Median			.9600	
Variance			2.254E-04	
Std. Deviation			1.501E-02	
Minimum			.91	
Maximum			.99	
Range			.08	
Interquartile Range			2.000E-02	
Skewness			-.537	.172
Kurtosis			.360	.342

Descriptive Statistics II

Descriptive Statistics

	MCLASS	Mean	Std. Deviation	N
TROCCRT	C	.9805	7.006E-03	121
	U	.9738	6.917E-03	79
	Total	.9779	7.694E-03	200
TREFFRT	C	.2032	5.448E-02	121
	U	.2017	4.458E-02	79
	Total	.2026	5.069E-02	200

Correlation Matrix

The Pearson correlation test for linearity between dependent variables is somewhat significant at 49%; this is also indicated in the scatter plots in the Appendix.

Correlations

		EFFRNTS TRU	OCCRTS TRUC
EFFRNTSTRU	Pearson Correlation	1.000	.488**
	Sig. (2-tailed)	.	.000
	N	200	200
OCCRTSTRUC	Pearson Correlation	.488**	1.000
	Sig. (2-tailed)	.000	.
	N	200	200

** . Correlation is significant at the 0.01 level (2-tailed).

Box's Test of Equality of Covariance Matrices

Box's test is not significant; therefore, Wilks' Lambda criteria is used to test group means.

Box's Test of Equality of Covariance Matrices^a

Box's M	23.117
F	7.616
df1	3
df2	1386223
Sig.	.000

Tests the null hypothesis that the observed covariance matrices of the dependent variables are equal across groups.

a. Design: Intercept+MCLASS

MANOVA Summary Table

Eta Square and F Statistics indicate that the classification (MCLASS) between constrained (C) and unconstrained (U) is statistically significant in affecting the combined dependent variables of structural effective rents and occupancy rates.

Multivariate Tests^b

Effect		Value	F	Hypothesis df	Error df	Sig.	Eta Squared
Intercept	Pillai's Trace	1.000	2527402 ^a	2.000	197.000	.000	1.000
	Wilks' Lambda	.000	2527402 ^a	2.000	197.000	.000	1.000
	Hotelling's Trace	25658.908	2527402 ^a	2.000	197.000	.000	1.000
	Roy's Largest Root	25658.908	2527402 ^a	2.000	197.000	.000	1.000
MCLASS	Pillai's Trace	.233	29.859 ^a	2.000	197.000	.000	.233
	Wilks' Lambda	.767	29.859 ^a	2.000	197.000	.000	.233
	Hotelling's Trace	.303	29.859 ^a	2.000	197.000	.000	.233
	Roy's Largest Root	.303	29.859 ^a	2.000	197.000	.000	.233

a. Exact statistic

b. Design: Intercept+MCLASS

MANOVA Tests Between-Subjects Effects

Significants and F test statistics indicate that the category of the submarket significantly affect occupancy rate, but it does not affect effective rents. This leads us to conclude that there are other unobserved variables with in the categorical analysis. Future research would require continued transformation of the effective rent variable, and to extend the analysis to MANCOVA, controlling for other variable influences.

Tests of Between-Subjects Effects

Source	Dependent Variable	Type III Sum of Squares	df	Mean Square	F	Sig.	Eta Squared
Corrected Model	TROCCRT	2.158E-03 ^a	1	2.158E-03	44.405	.000	.183
	TREFFRT	9.623E-05 ^b	1	9.623E-05	.037	.847	.000
Intercept	TROCCRT	182.550	1	182.550	3756530	.000	1.000
	TREFFRT	7.835	1	7.835	3034.718	.000	.939
MCLASS	TROCCRT	2.158E-03	1	2.158E-03	44.405	.000	.183
	TREFFRT	9.623E-05	1	9.623E-05	.037	.847	.000
Error	TROCCRT	9.622E-03	198	4.860E-05			
	TREFFRT	.511	198	2.582E-03			
Total	TROCCRT	191.260	200				
	TREFFRT	8.720	200				
Corrected Total	TROCCRT	1.178E-02	199				
	TREFFRT	.511	199				

a. R Squared = .183 (Adjusted R Squared = .179)

b. R Squared = .000 (Adjusted R Squared = -.005)

Concluding Remarks

Overall, apartment markets in the West have gone through many cycles over the past 19 years, and will continue to go through cycles in the future. However, in the past, where most metro area apartment markets in the West would go through their cycles together, in the 1970s and 1980s, they are now, in the 1990s and 2000s, going through their cycles independently and with less risk of overbuilding.

Supply-constrained markets tend to be more stable over the long-run and experience longer and shallower cycles when compared to supply-unconstrained markets. Although supply-constrained markets are projected to outperform supply-unconstrained markets in the future, the majority of supply-unconstrained markets in the West are projected to see above inflation effective rent growth and healthy rates of total return.

Building a Western focused portfolio of supply-constrained and supply-unconstrained markets provides for greater geographical and economic diversification and higher total returns over the long-run, without having to go to a national strategy.

As the apartment sector continues to move from private to public ownership, and as the capital markets play a larger roll in allocating development capital, supply-unconstrained markets in the West will start to take on supply-constrained market characteristics. This, in the long-run, should smooth out the cycles of severe over and under supply, extend the cycles out farther into the future, and provide higher rates of return in the long-run.

CONTRIBUTION TO DISCIPLINE

The two main contributions this research provides to the discipline are: 1) the development of a total apartment return forecast model for each metro area in the Western region and 2) the application of MPT to real real estate portfolios.

Economic Base Diversification and Portfolio Optimization

The real contribution to the discipline is the combination of economic base diversification and portfolio optimization. This approach to portfolio diversification and optimization uses passive and active management strategy or style.

The passive approach is to index the portfolio according to the distribution of industry employment across the western region, and the active approach is to look at employment trends by industry across the western region.

The active approach using the Markowitz Model substitutes metro areas in the geographic model industries in the economic model. Industries consist of 13 economic based categories that have already been developed for the Western Region by Regional Financial Associates. These industries include technology, durable goods, high technology, government, gaming, hotels and resorts, etc.

The economic base model allows the use of basically the same structural model used for the geographic diversification model. The research looks at industries within the Western Region instead of metro areas, answering the question "How do you want to distribute or optimize the portfolio across industries?"

Once the optimal allocation by industry category has been determined, the portfolio can be analyzed for how it is distributed by industry. From this analysis, I can identify where we are over and under concentrated by industry, then identify what metro areas the REIT would want to enter to balance out the portfolio's economic concentration.

Geographic and economic base diversification and optimization results were reconciled. The geographics tells how the portfolio should distributed geographically and the economics tells how the REIT should be distributed economically. For example, using economic base diversification with a passive style, the portfolio is over concentrated in high tech, but the portfolio may be under-concentrated in durable goods manufacturing. To diversify the portfolio the REIT would want to invest in a metro area with a high concentration of durable goods manufacturing, Denver and Seattle.

The goal of this strategy is to look towards markets understanding how they are over and under-concentrated by industry and how the REIT wants to allocate our assets. The REIT is looking at the portfolio from both its geographic distribution and the characteristics of individual metro areas by industry. For example, right now the REIT portfolio is over concentrated in the Bay Area and in high-tech using the passive portfolio approach. This information and research is valuable to the REIT portfolio manager and contributes significantly to the discipline.

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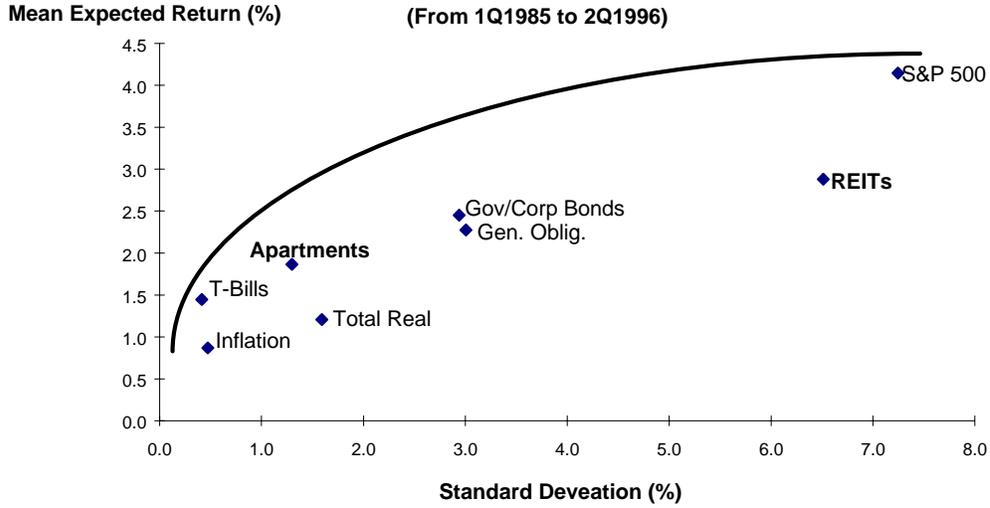
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APPENDICIES

APPENDIX I

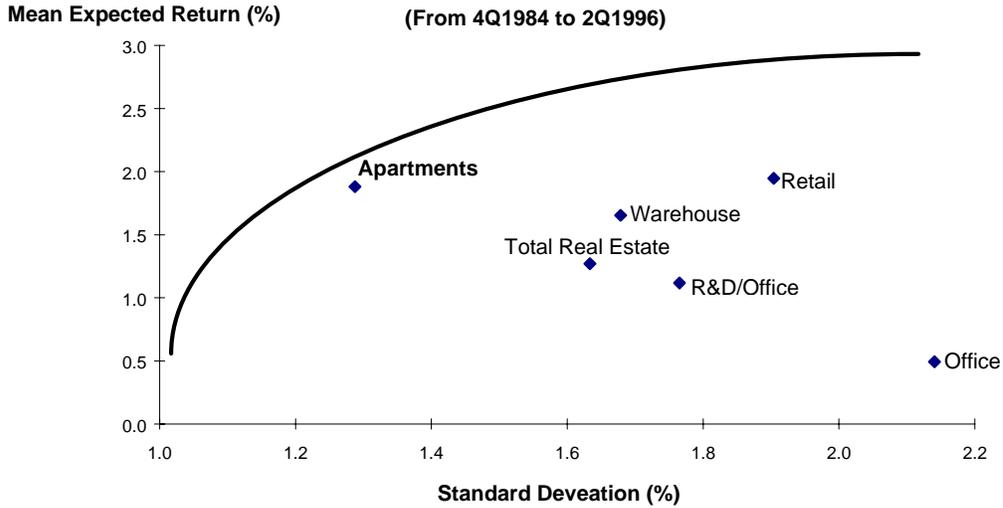
REAL ESTATE IN A CAPITAL MARKETS CONTEXT

**CAPITAL MARKET ANALYSIS
COMPETITIVE ASSET CLASSES
EFFICIENT FRONTIER
(From 1Q1985 to 2Q1996)**

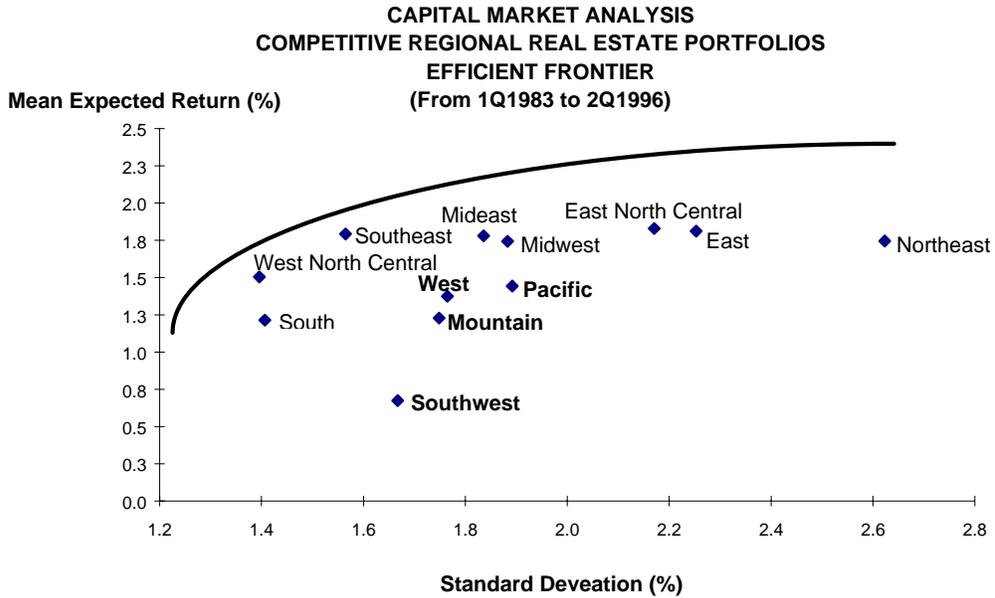


Source: NCREIF Property Index Detailed Quarterly Performance Report and BRE Properties Research Dept.

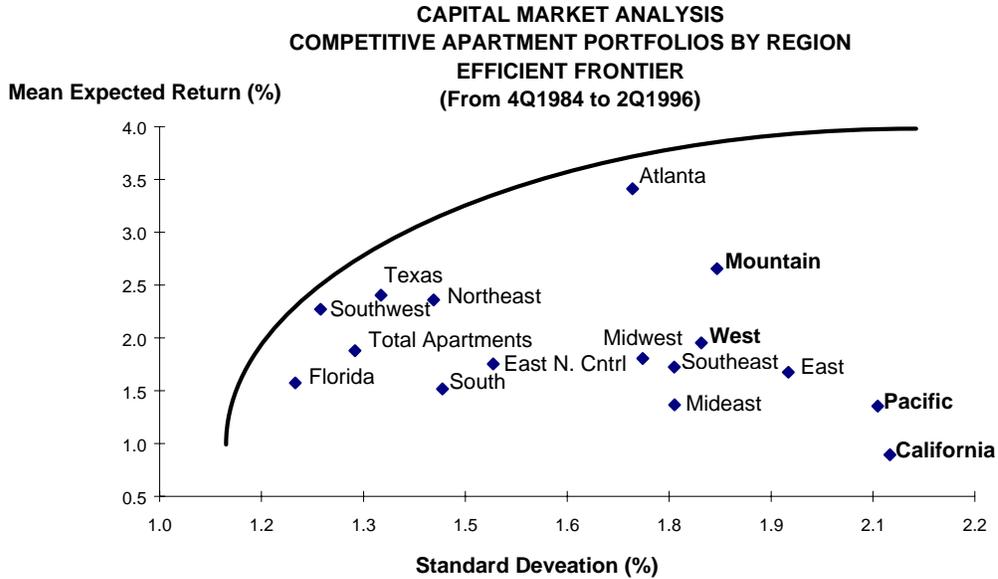
**CAPITAL MARKET ANALYSIS
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EFFICIENT FRONTIER
(From 4Q1984 to 2Q1996)**



Source: NCREIF Property Index Detailed Quarterly Performance Report and BRE Properties Research.

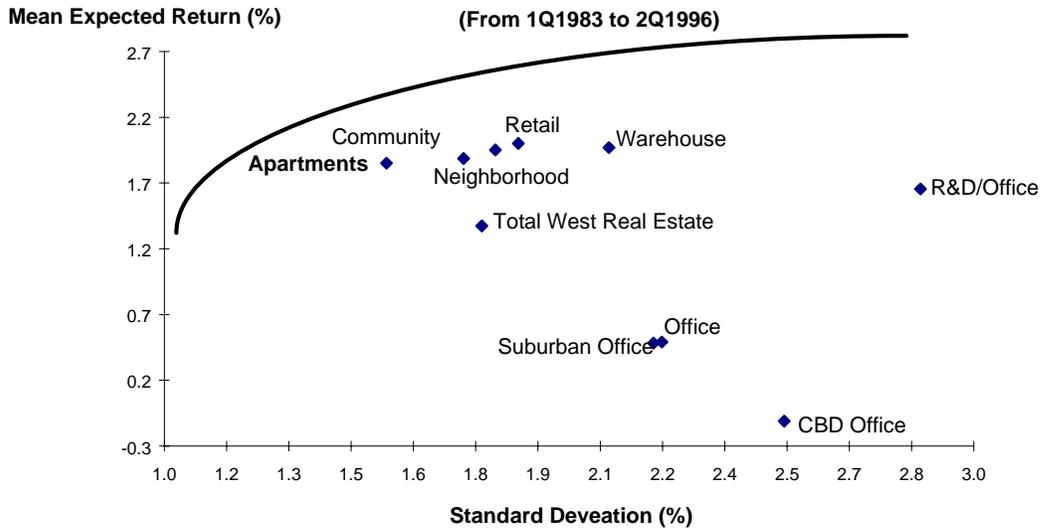


Source: NCREIF Property Index Detailed Quarterly Performance Report and BRE Properties Research.



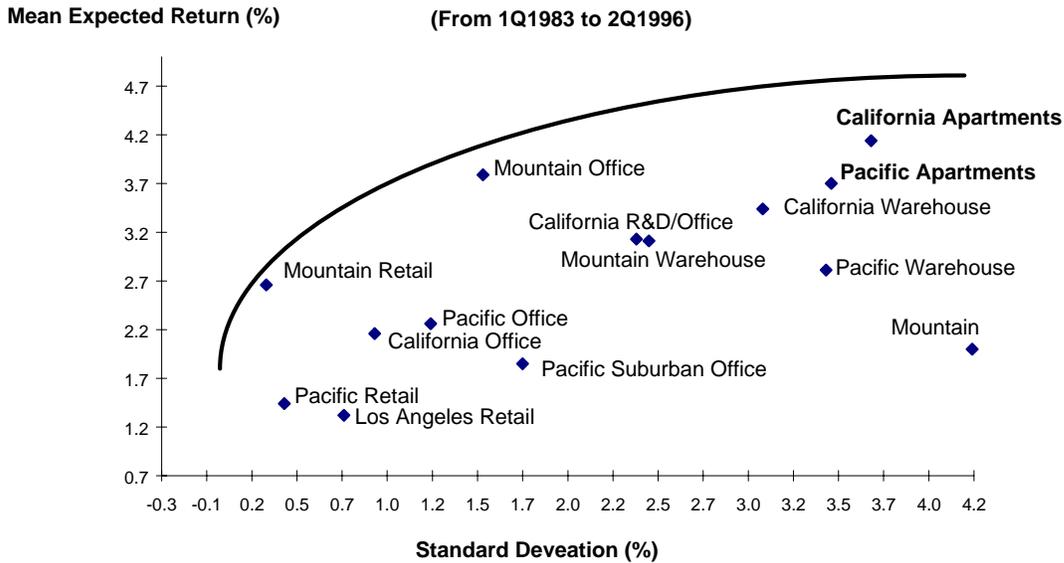
Source: NCREIF Property Index Detailed Quarterly Performance Report and BRE Properties Research.

**CAPITAL MARKET ANALYSIS
COMPETITIVE REAL ESTATE PORTFOLIOS IN THE WESTERN REGION
EFFICIENT FRONTIER
(From 1Q1983 to 2Q1996)**



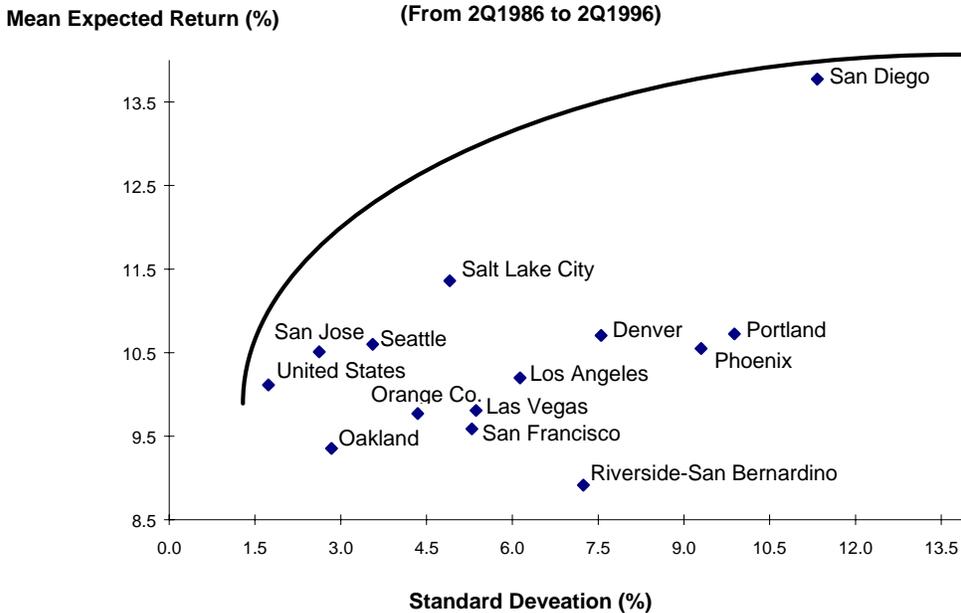
Source: NCREIF Property Index Detailed Quarterly Performance Report and BRE Properties Research.

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COMPETITIVE REAL ESTATE PORTFOLIOS BY WESTERN REGIONS
EFFICIENT FRONTIER
(From 1Q1983 to 2Q1996)**



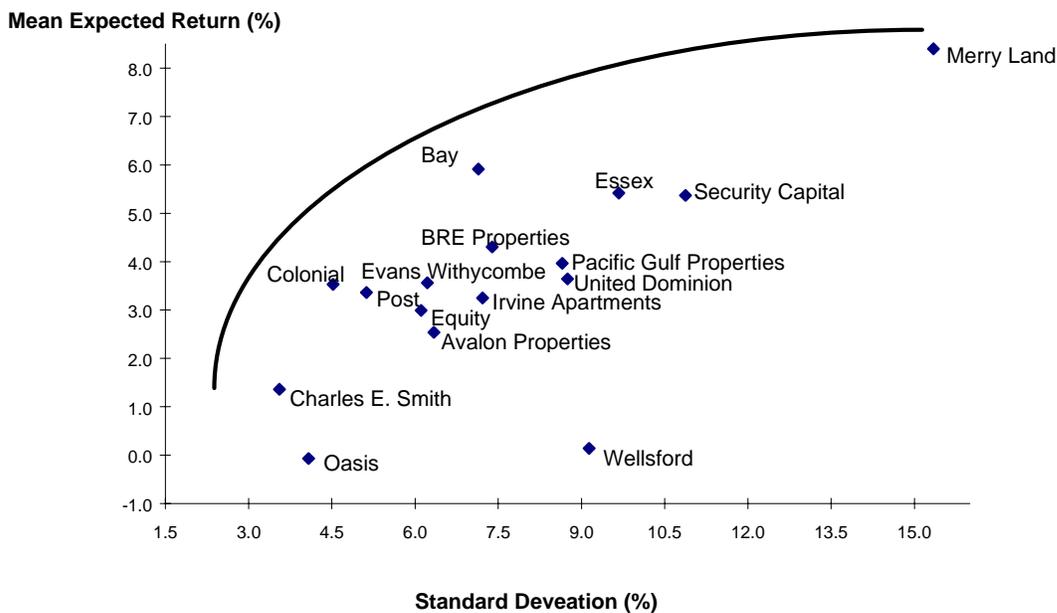
Source: NCREIF Property Index Detailed Quarterly Performance Report and BRE Properties

**CAPITAL MARKET ANALYSIS
COMPETITIVE METROPOLITAN APARTMENT PORTFOLIOS IN THE WESTERN REGION
EFFICIENT FRONTIER
(From 2Q1986 to 2Q1996)**



Source: The National Real Estate Index and BRE Properties Research Department.

**CAPITAL MARKET ANALYSIS
COMPETITIVE APARTMENT REIT PORTFOLIOS
EFFICIENT FRONTIER**



Source: Dean Witter Reynolds Investment Banking and and BRE Properties Research.

APPENDIX II

General Industry Categories

Economic Base Concentration by Metro Area

Expected Portfolio Composition

APPENDIX III

BACK TESING THE FORECAST MODEL

Summary Table and Individual Market Results

Example: Metro Rankings Over Time

- Individual Market Results

Note: The Individual Market Graph and Table identifies the degree to which the forecast model predicted movements in rankings over time, given that the forecast rank fell within four ranks from the actual.

For Example:

The *Denver Graph* shows that 85% of the time, the Forecast Model predicted total return rankings which corresponded to actual apartment returns, effective rent growth and vacancy rate rankings—falling well within an error tolerance level of 0 – 4 ranks; and of this 85%, 80% fell within 0 – 2 ranks and 20% fell within 3 – 4 ranks.

The *Denver Table* shows that the model predicted actual apartment return rankings roughly 100% of the time; effective rent growth rankings roughly 90% of the time; and vacancy rate rankings roughly 65% of the time.

Metro area pages have been sorted by degree of forecast accuracy.

APPENDIX IV

QUALITATIVE FACTORS

PORTFOLIO ATTRIBUTES

CORE MARKET CHARACTERISTICS

MARKET SUMMARIES

MARKET EXIT CONSIDERATIONS

APPENDIX V

RISK/RETURN SENSITIVITY ANALYSIS: MARKOWITZ OPTIMIZATIONS

APPENDIX VI

REGRESSION ANALYSIS:

PREDICTING TOTAL APARTMENT RETURN BY METRO AREA

APPENDIX VII

TOTAL RETURN GRAPHS

TOTAL RETURN DEVIATION GRAPHS

APPENDIX VIII

TABLES SORTED BY:

**RISK-ADJUSTED RETURN
EXPECTED RETURN
AND STANDARD DEVIATIONS**

APPENDIX IX

STATISTICAL RULES OF THUMB

The one variable linear regression model: $Y_i = \beta_0 + \beta_1 X_i + u_i$

where: β_0 = the intercept, it is an average level of return if the X coefficient is zero

β_1 = the explanatory X variable, or slope coefficient. It measures the rate of change in the conditional mean value of Y_i per unit change in X

u_i = the stochastic, residual, or the random error term, the error term may represent the influence of those that are not explicitly in the model, even if we included all variables that determine Y levels, some “intrinsic randomness” is bound to occur that cannot be explained, no matter how hard we try.

Y_i = the dependent Y variable, the average response value for a given level of the X coefficient.

Insert Norm. equation here?

Any linear function of a normally distributed variable is itself normally distributed, which means there is a high degree of predictability of returns in the regression model.

If the distributions of the explanatory (X) variables are normally distributed, then the Markowitz Mean-Variance criterion can be used to achieve an optimal decision.

Correlation coefficient: is a measure of linear association between two variables, the coefficient lies between 1 and -1 . Positive 1 means if one variable goes up, the other goes up equally. Conversely, negative correlation implies that if one variable goes up, the other goes down by equal measure.

Statistical independence: a measure of the relationship between two variables. In practice, the returns on two metro markets, i.e. X variables need not be completely independent. As long as they are not *perfectly* correlated there will be gains from diversification in the portfolio. (Haim 287)

If correlations among explanatory variables are high (in excess of .8) then there is the possibility that some collinearity (very high similarity) among explanatory variables exists (p.299). In cases of high collinearity it is futile to assess the contribution of each explanatory variable to the overall R^2

Nonstochastic means constant.

No auto correlation means that the error terms of the regression, the u_i 's are random

-The Durbin-Watson statistic is a number generated by the statistical software package that indicates whether or not this problem is present in the data.

DW = 4 indicates evidence perfect negative autocorrelation

DW = 2 (or close to 2) **no autocorrelation**, it is safe to trust the regression coefficients

DW = 0 indicates evidence of positive autocorrelation

Multiple Regression

$$E(Y_i) = \beta_1 + \beta_2 X_{2t} + \beta_3 X_{3t} + u_t$$

where: B_2 and B_3 are known as partial regression or partial slope coefficients. Partial's meaning is as follows: B_2 measures the expected change in the mean value of Y, $E(Y)$, per unit change in X_2 , holding the value of X_3 constant. The same rule applies for B_3 .

R-Squared (“Goodness of Fit” of the regression line to the data)

r^2 , the coefficient of determination, measures the percentage of total variation in Y explained by the single explanatory (X) variable regression model.

R^2 , the multiple coefficient of determination, measures the percentage of total variation explained by X_2 and X_3 jointly, in a multiple regression model.

ESS = Explained (by the regression) sum of squares

RSS = Residual (or unexplained) sum of squares variation of Y values around the regression line

TSS = Total sum of squares; TSS=ESS+RSS

Range of $r^2 = 0 \leq r^2 \leq 1$; 1 indicates a perfect fit and 0 indicates no relationship whatsoever

$$1 = \frac{ESS}{TSS} + \frac{RSS}{TSS} \qquad r^2 = \frac{ESS}{TSS}$$

Normality

$X \sim N(\mu, \sigma^2)$, where \sim means “distributed as,” N stands for normal distribution, and the quantities inside the parenthesis are the parameters of the distribution, i.e. its mean (or expected value) and its variance.

Properties of the Normal Distribution

1. The normal distribution curve is symmetrical around its mean value, μ .
2. The probability of obtaining a value of a normally distributed random variable far away from its mean becomes progressively smaller.
3. Approximately 68% of the area under the normal curve lies between plus or minus one standard deviation from the mean; 95% of the area lies between plus or minus two standard deviations from the mean; and 99.7% of the area lies between plus or minus three standard deviations from the mean.
4. A normal distribution is fully described by its two parameters, μ and σ^2 . That is, once these parameter values are known one can find the probability of X lying within a certain interval.
5. A linear combination of two or more normally distributed random variables is itself normally distributed, which means there is a high degree of predictability of returns in the regression model.

An Insignificant t stat yet overall high correlation

If there is an insignificant variable (low t statistic) in the multiple regression model that should be included because of economically intuitive reasons, the software will calculate a smaller coefficient for the insignificant t statistic. For example, with the employment and population variables highly significant and multifamily housing permits insignificant, the software will calculate a regression equation $7.16 + 5.24*EMPL + 12.3*POP + .00125*MPERM$. In other words, the computer will compensate in order to maintain a high correlation in the overall regression model with high F scores.

F ratio

The F ratio [(regression mean square) / (residual mean square)] should exceed the factor, i.e. score of four in order for the regression to be predictive.

APPENDIX X

DEFINITIONS AND DATA SOURCES